

# EC 744 Wireless Communications Spring 2007

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Department of Electronics and Communications

## Digital Modulation Techniques

**[WWW.aast.edu/~khedr/Courses](http://WWW.aast.edu/~khedr/Courses)**

# Syllabus

- Tentatively

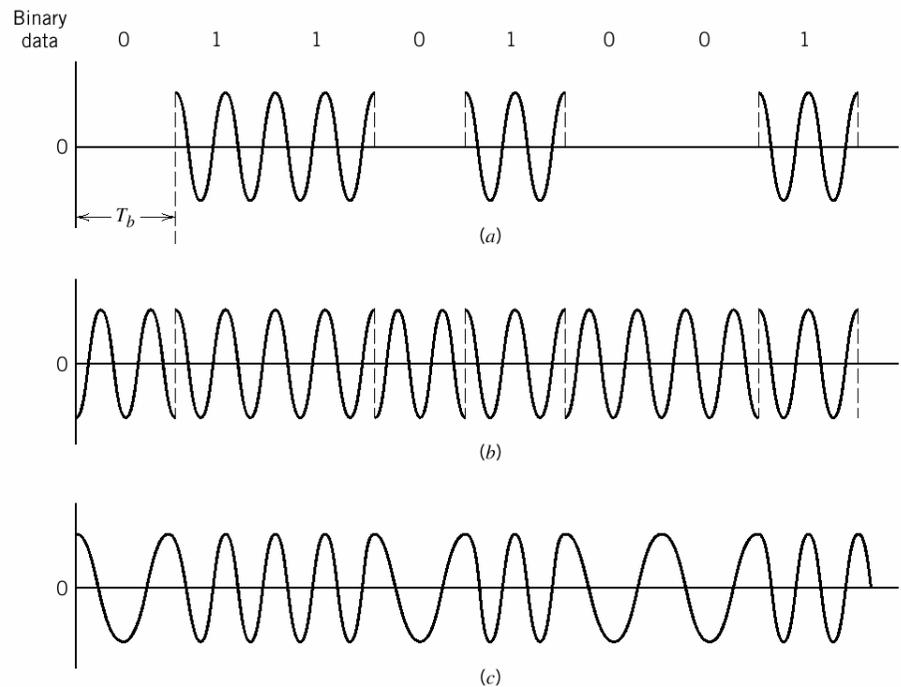
Week 1	Overview, Probabilities, Random variables, Random process
Week 2	Wireless channels, Statistical Channel modelling, Path loss models
Week 3	Cellular concept and system design fundamentals
Week 4	Modulation techniques, single and multi-carrier
Week 5	Diversity techniques
Week 6	Equalization techniques
Week 7	Mid Term exam
Week 8	802.11 and Mac evaluation
Week 9	Energy models in 802.11
Week 10	Wimax and Mac layer
Week 11	Presentations
Week 12	Presentations
Week 13	Presentations
Week 14	Presentations
Week 15	Final Exam

# Chapter 6

## Passband Data Transmission

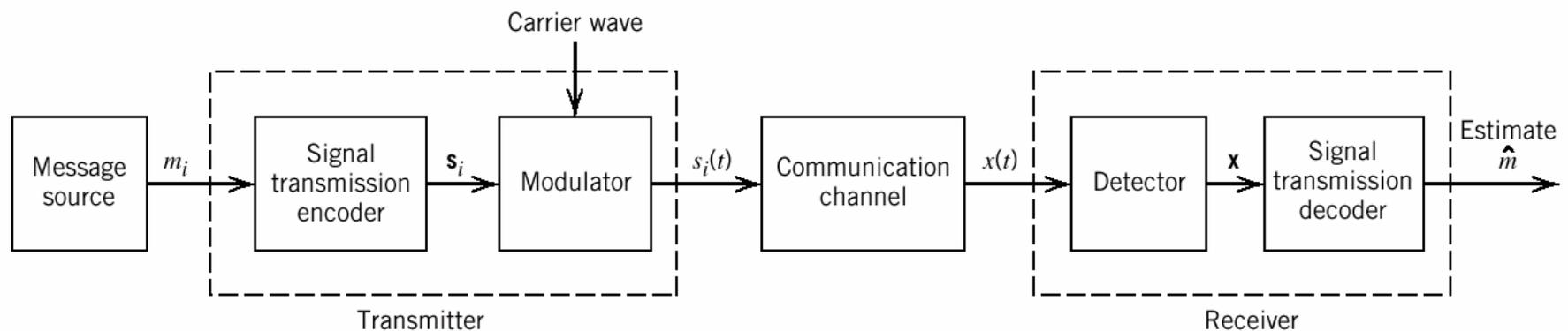
# Figure 6.1

Illustrative waveforms for the three basic forms of signaling binary information. (a) Amplitude-shift keying. (b) Phase-shift keying. (c) Frequency-shift keying with continuous phase.



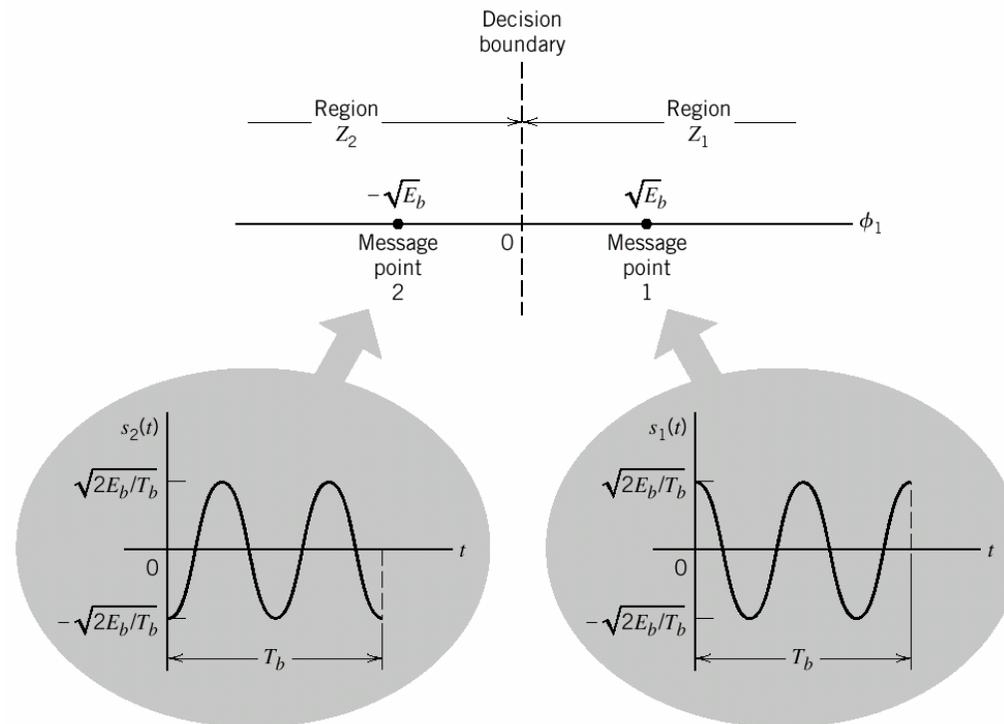
# Figure 6.2

Functional model of passband data transmission system.



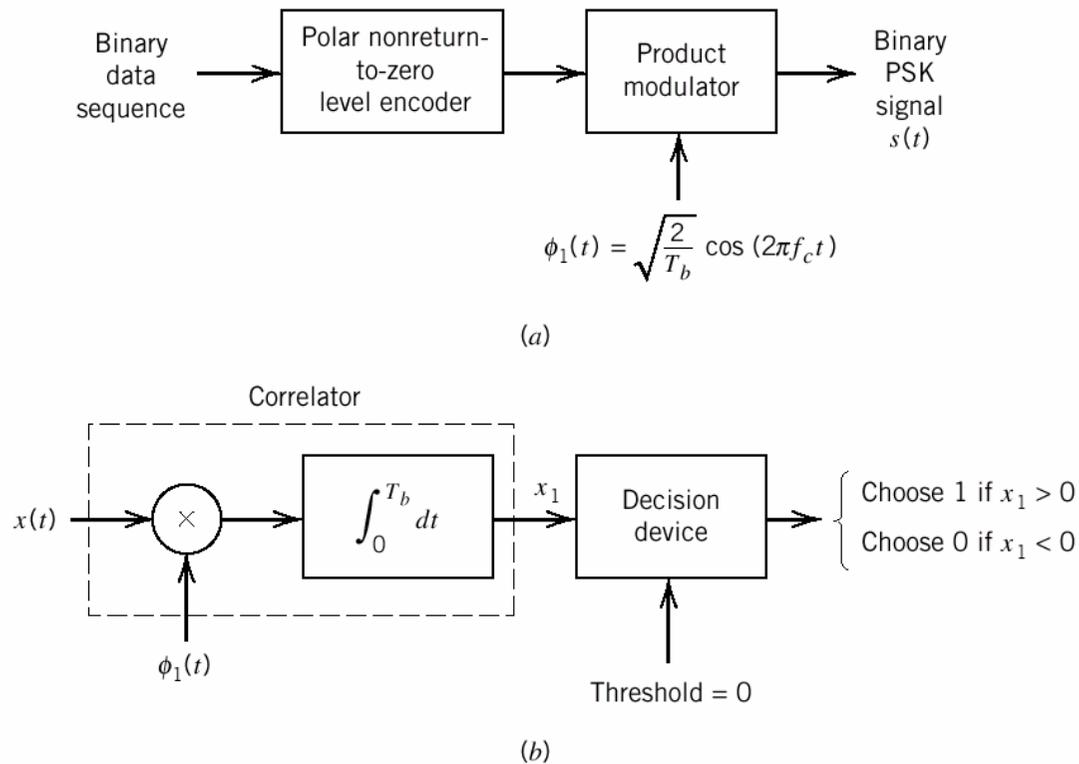
# Figure 6.3

Signal-space diagram for coherent binary PSK system. The waveforms depicting the transmitted signals  $s_1(t)$  and  $s_2(t)$ , displayed in the inserts, assume  $n_c = 2$ .



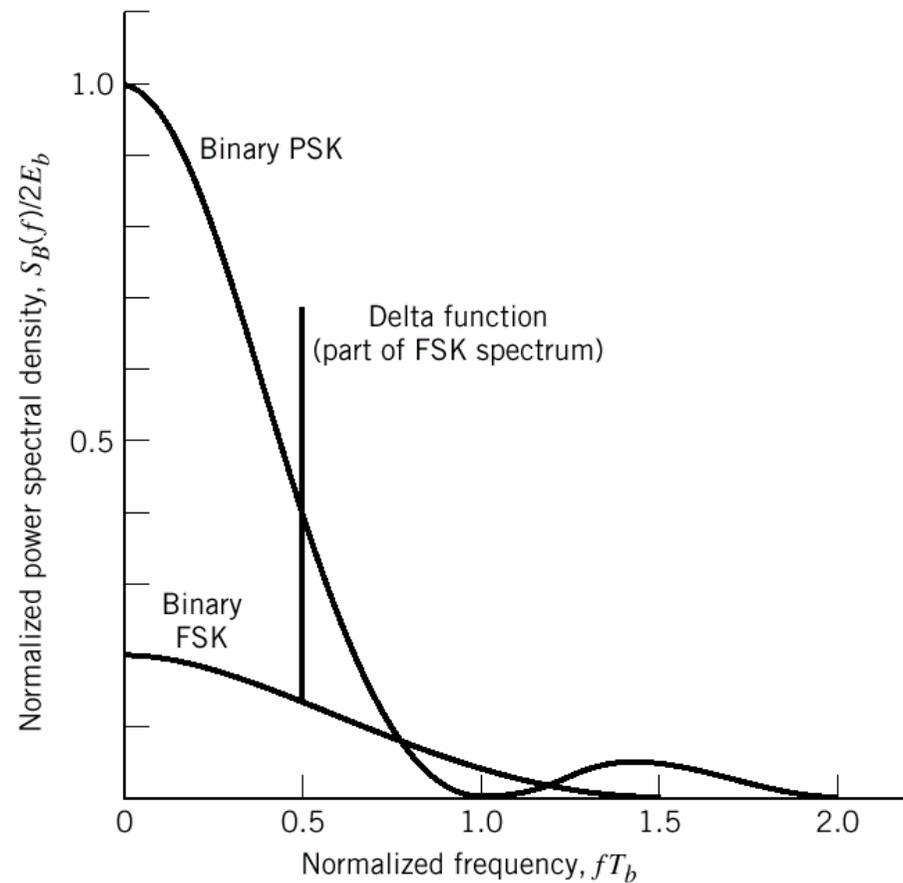
# Figure 6.4

Block diagrams for (a) binary PSK transmitter and (b) coherent binary PSK receiver.



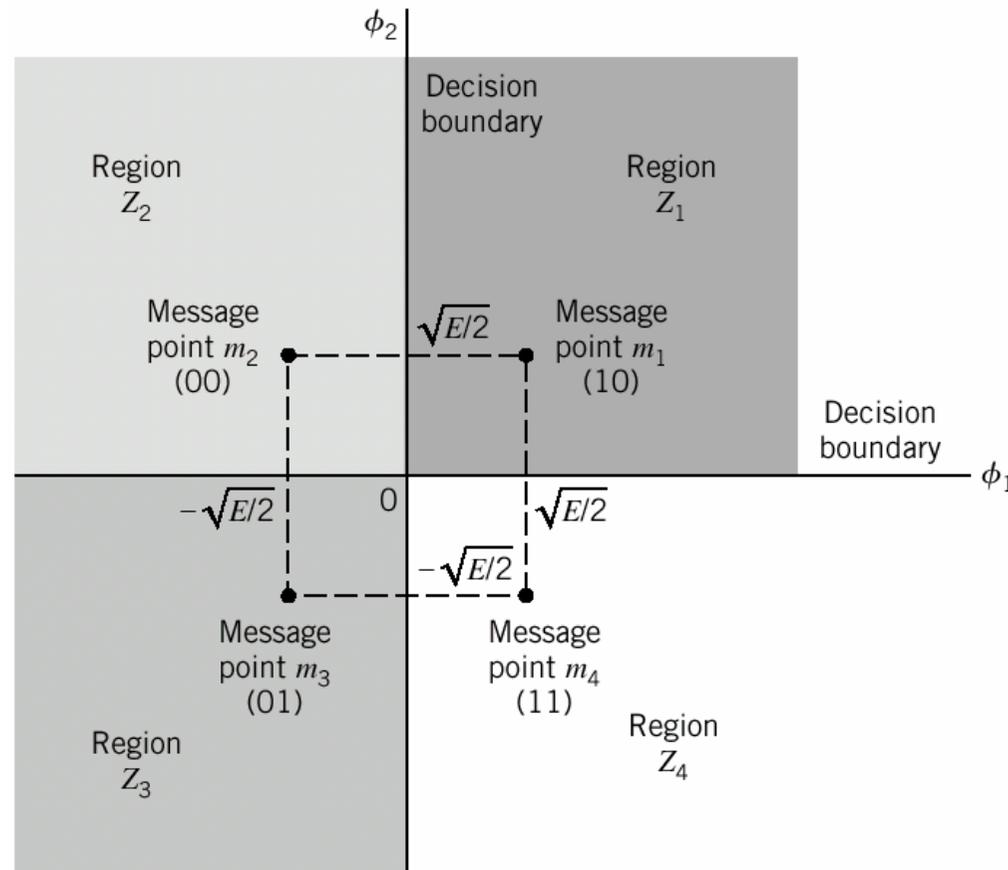
# Figure 6.5

Power spectra of binary PSK and FSK signals.



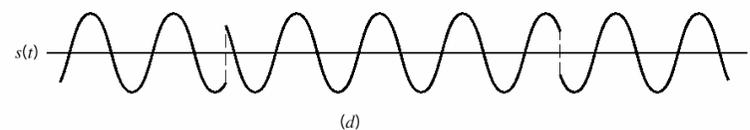
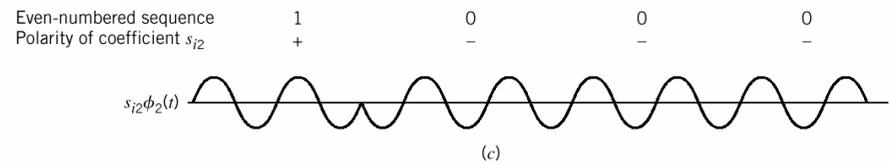
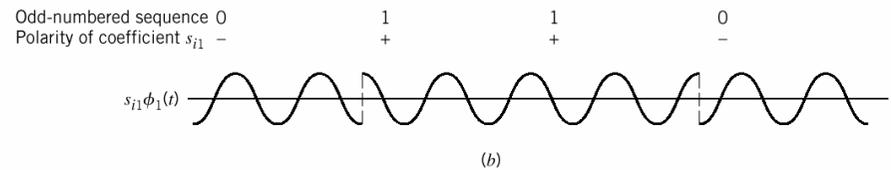
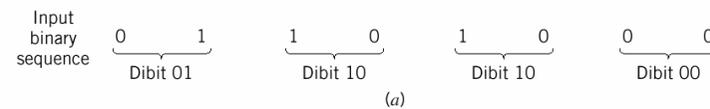
# Figure 6.6

Signal-space diagram of coherent QPSK system.



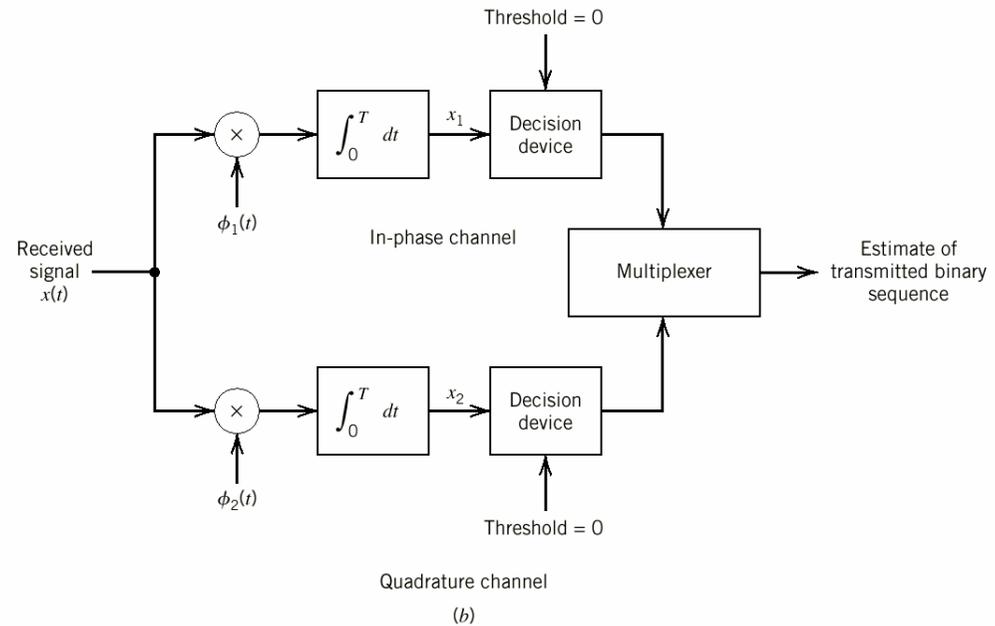
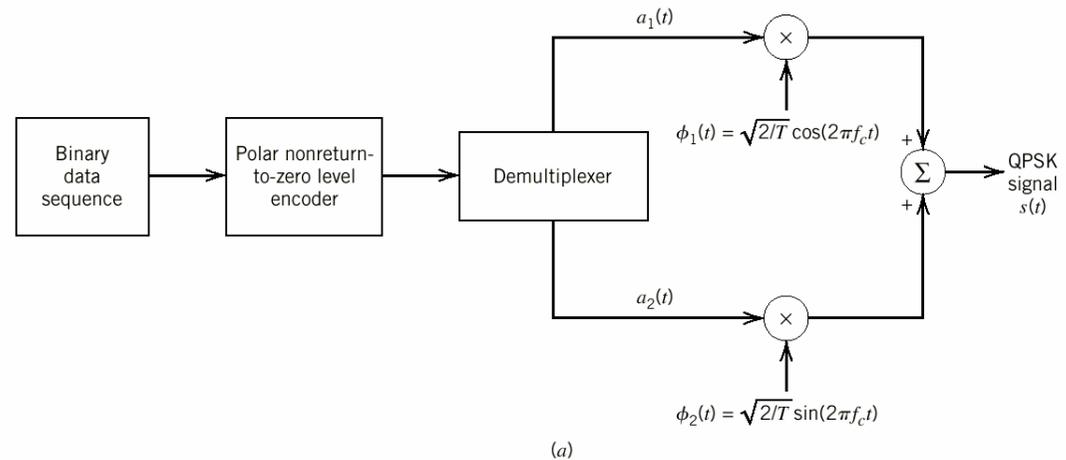
# Figure 6.7

(a) Input binary sequence. (b) Odd-numbered bits of input sequence and associated binary PSK wave. (c) Even-numbered bits of input sequence and associated binary PSK wave. (d) QPSK waveform defined as  $s(t) = s_{i1}\phi_1(t) + s_{i2}\phi_2(t)$ .



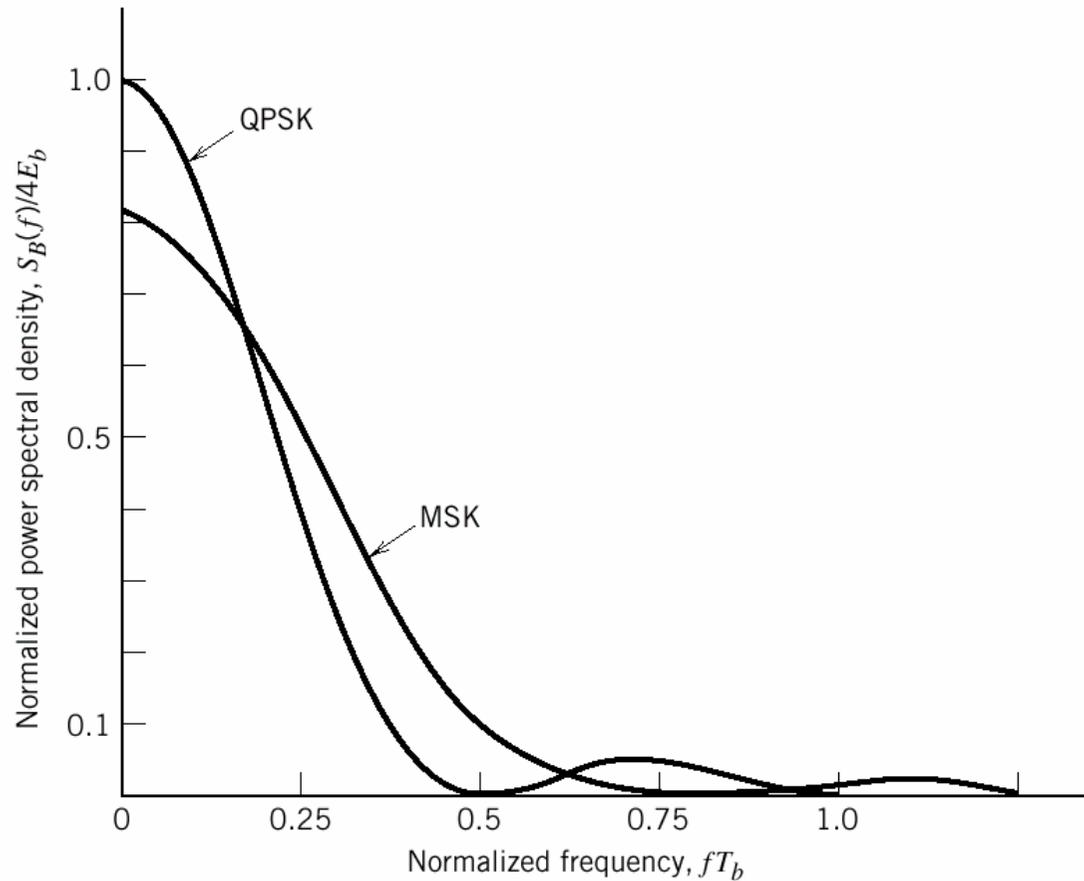
# Figure 6.8

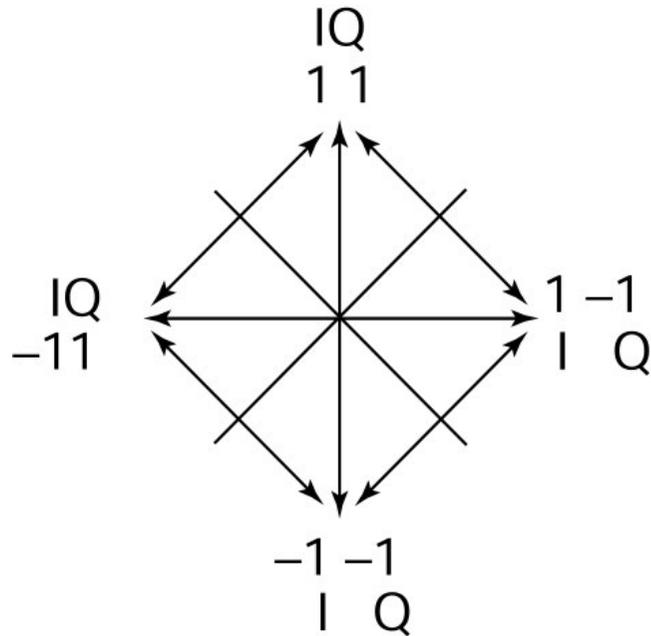
Block diagrams of (a) QPSK transmitter and (b) coherent QPSK receiver.



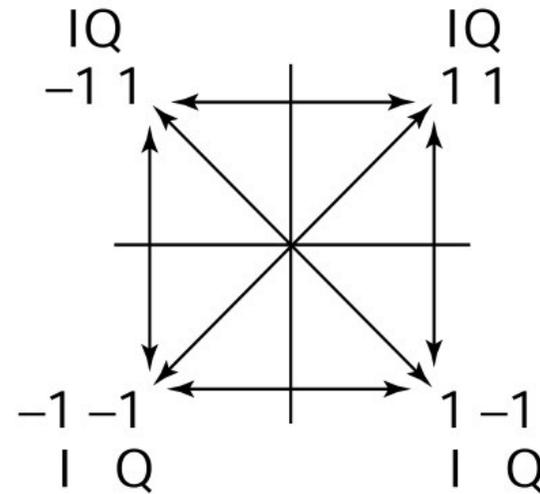
# Figure 6.9

Power spectra of QPSK and MSK signals.





(a) QPSK



(b) QPSK (carrier shifted by  $\pi/4$ )

The two QPSK constellations. Note that they differ by  $\pi/4$ . When going from (1,1) to (-1, -1), the phase is shifted by  $\pi$ . When going from (1, -1) to (1,1), the phase shifts by  $\pi/2$ . Thus, depending on the incoming symbol, transitions from (1,1) can occur to (1,1), (1,-1), (-1, 1), or (-1, -1) or vice versa, leading to phase shifts of  $0, \pm \pi/2, \text{ or } \pm \pi$  in QPSK. I and Q represent the in-phase and quadrature bits, respectively. Arrows show all possible transitions.

The pairing of bits to form symbols.

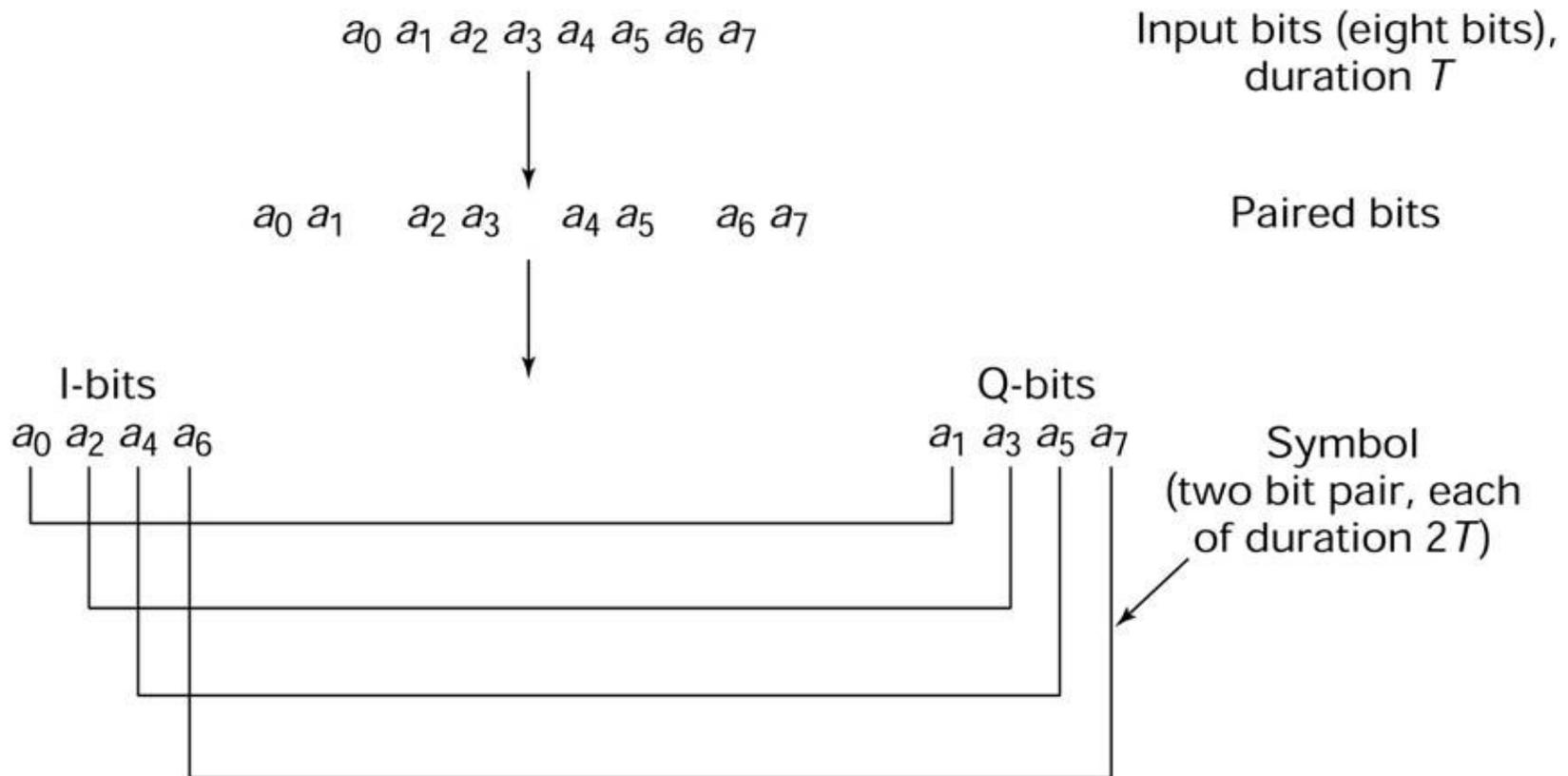


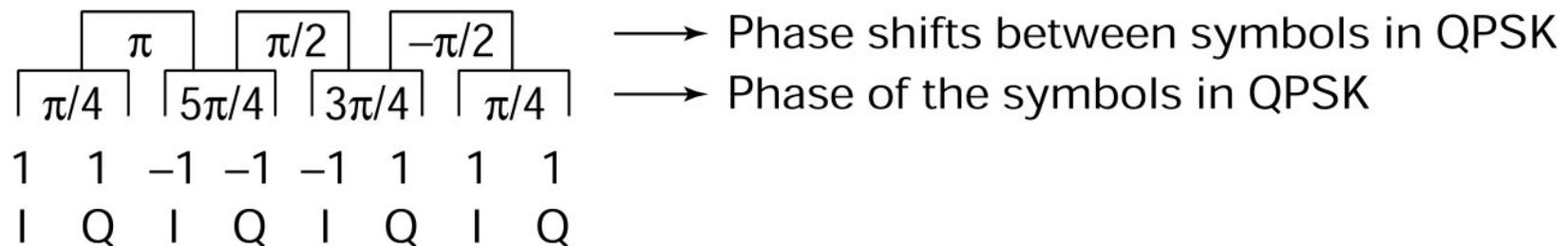
Figure 3.36. Explanation of the phase shifts observed in QPSK, indicating the phases of the symbols and the phase difference between symbols.

What happens to the phase at intervals of  $2T$  in QPSK?

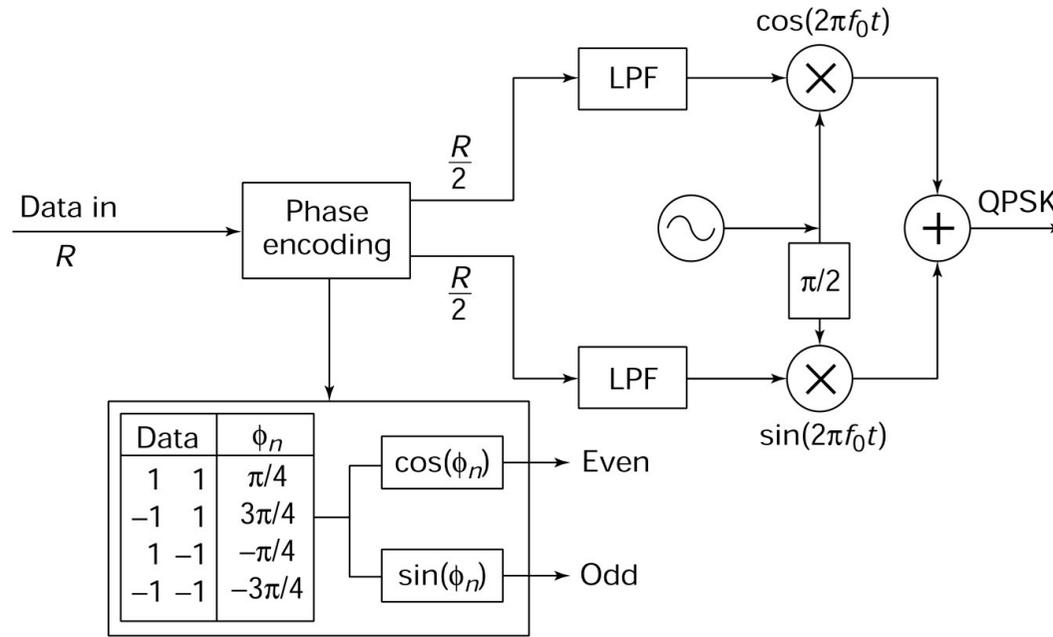
Phases of the symbols: All possible combinations:

1 1  $\longrightarrow$   $\pi/4$     -1 1  $\longrightarrow$   $3\pi/4$     -1 -1  $\longrightarrow$   $5\pi/4$     1 -1  $\longrightarrow$   $7\pi/4$

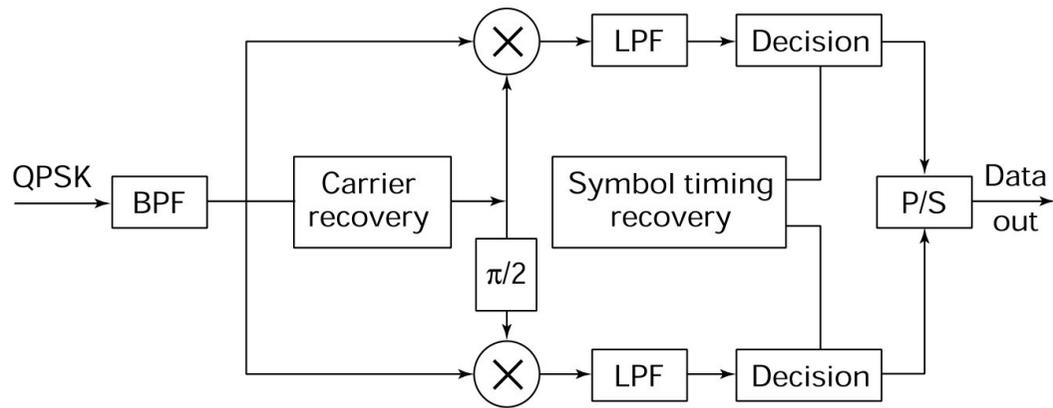
The bit stream is 1 1 -1 -1 -1 1 1 1.



**Figure 3.37.**  
 (a) QPSK transmitter. (b)  
 QPSK receiver.



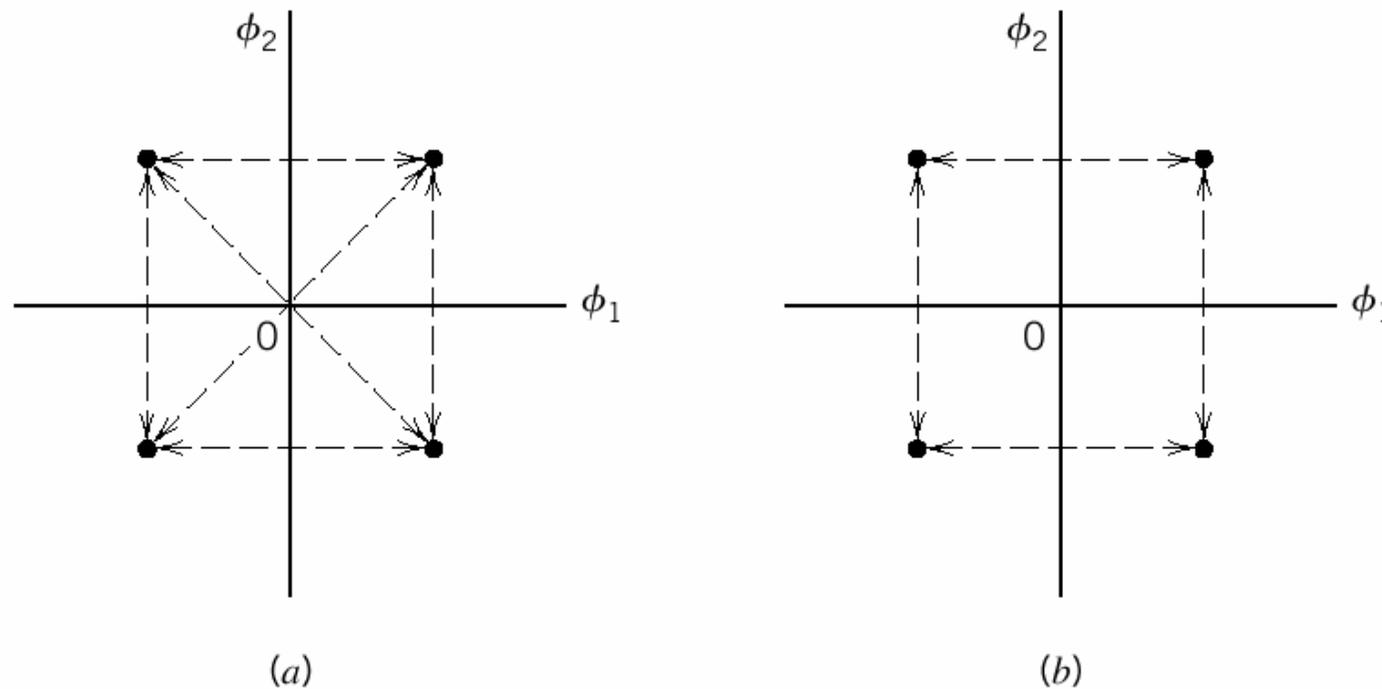
(a)



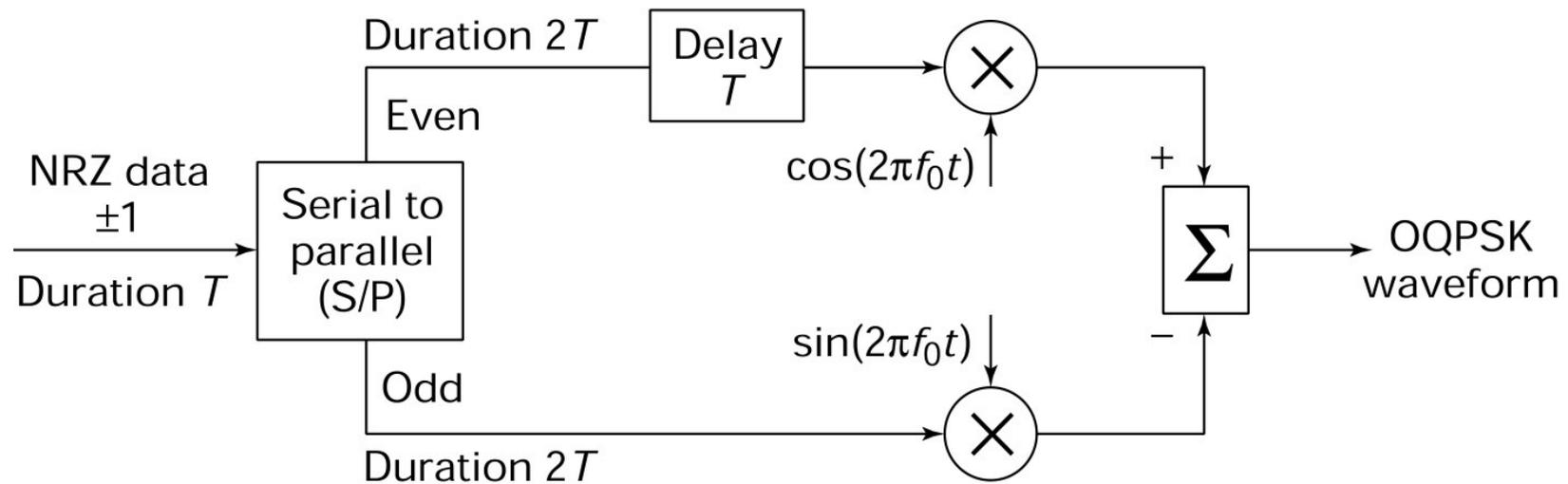
(b)

# Figure 6.10

Possible paths for switching between the message points in (a) QPSK and (b) offset QPSK.

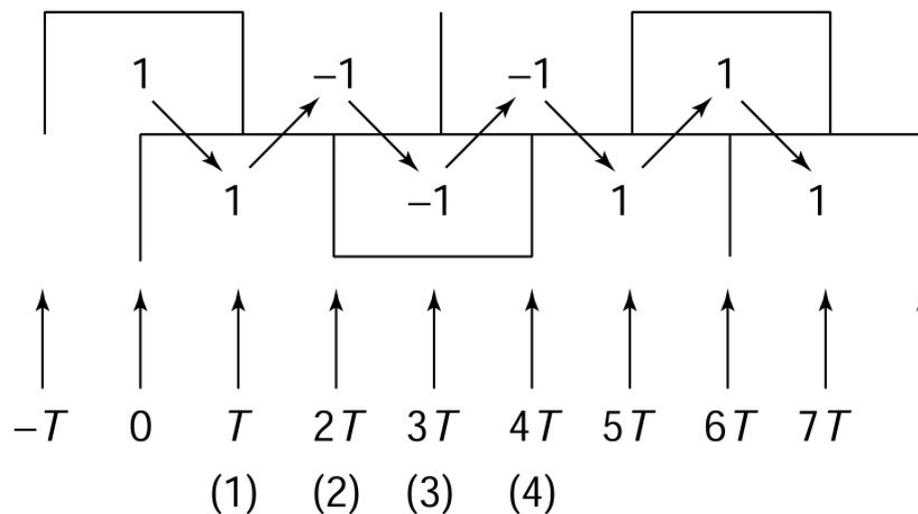


Block diagram of the OQPSK modulator.



## Explanation of the phase transitions in OQPSK.

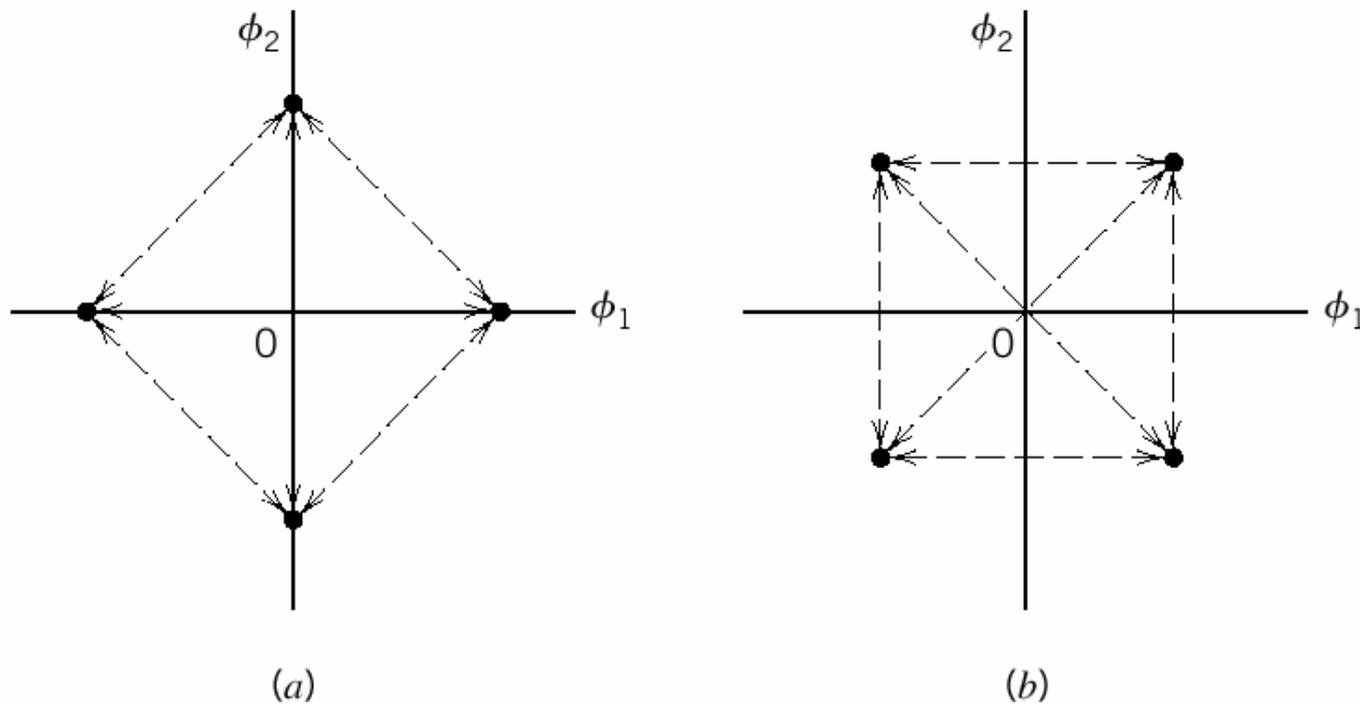
What happens to the phase at intervals of  $T$  in OQPSK



At (1), the symbols are (1, 1) and (-1, 1): The phase change is  $\pm\pi/2$ .  
At (2), the symbols are (-1, 1) and (-1, -1): The phase change is  $\pm\pi/2$ .  
At (3), the symbols are (-1, -1) and (-1, -1): The phase change is 0.  
At (4), the symbols are (-1, -1) and (-1, 1): The phase change is  $\pm\pi/2$ , and so on.  
Thus in OQPSK, the phase changes are limited to 0 or  $\pm\pi/2$ .

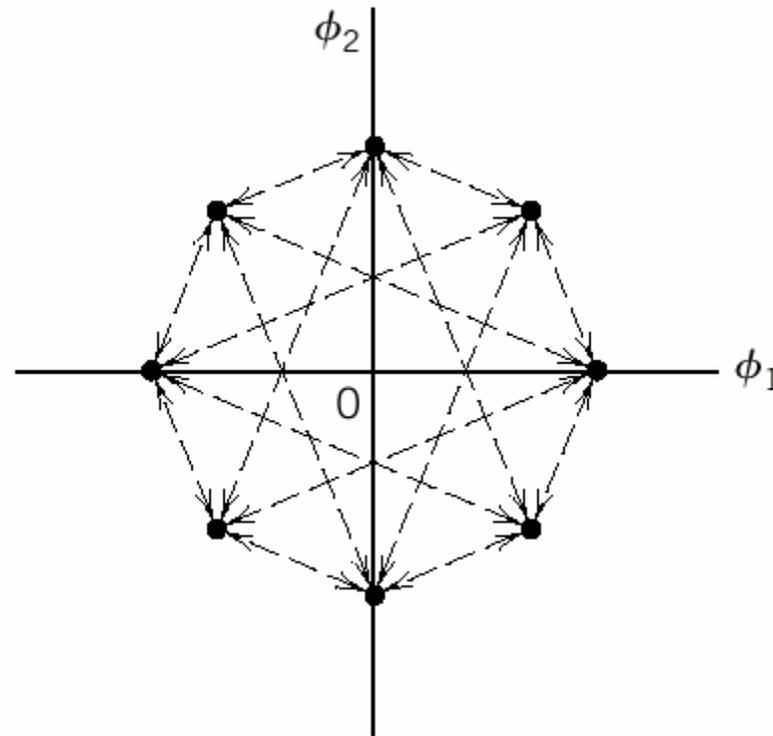
# Figure 6.11

Two commonly used signal constellations of QPSK; the arrows indicate the paths along which the QPSK modulator can change its state.

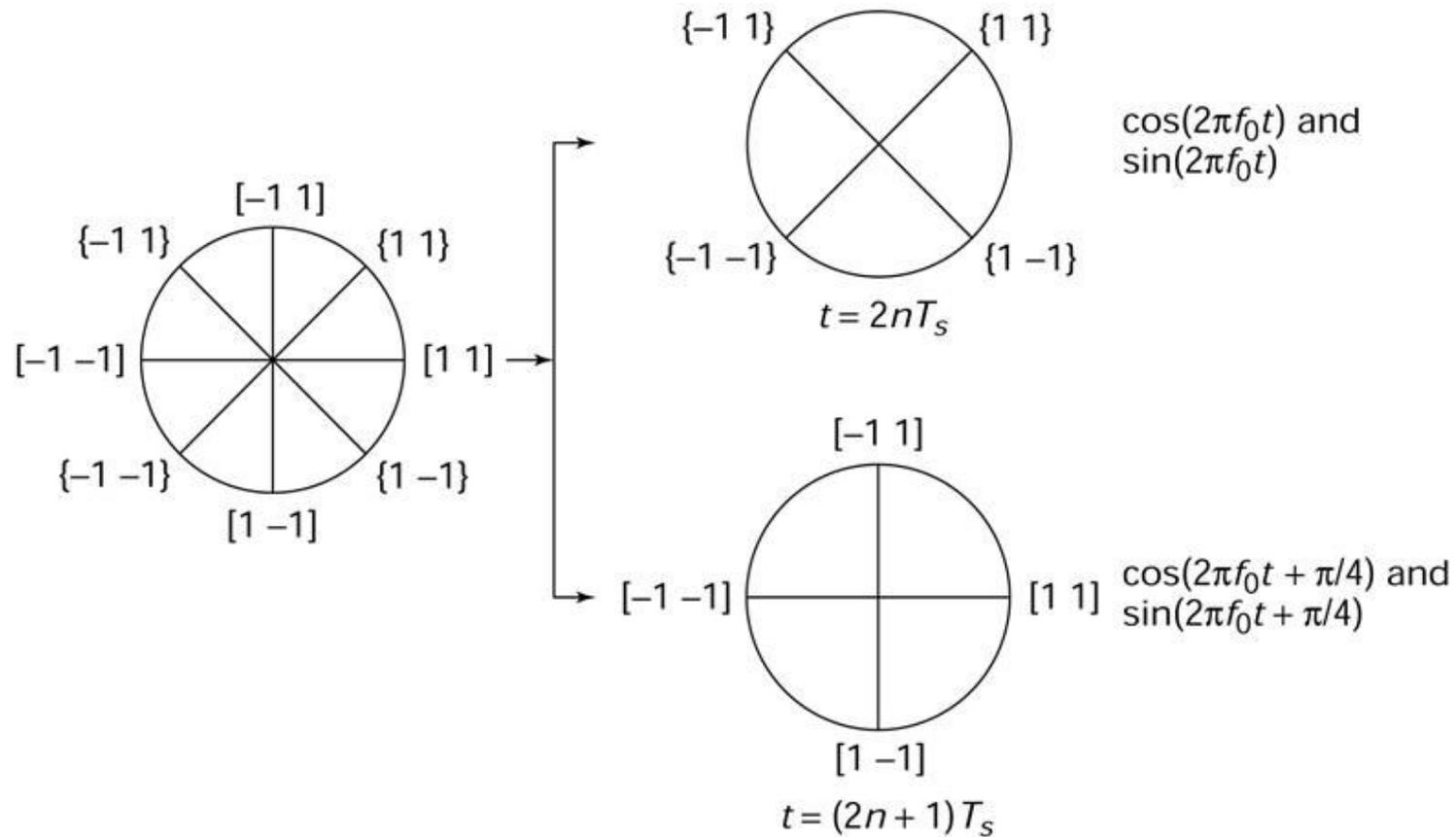


# Figure 6.12

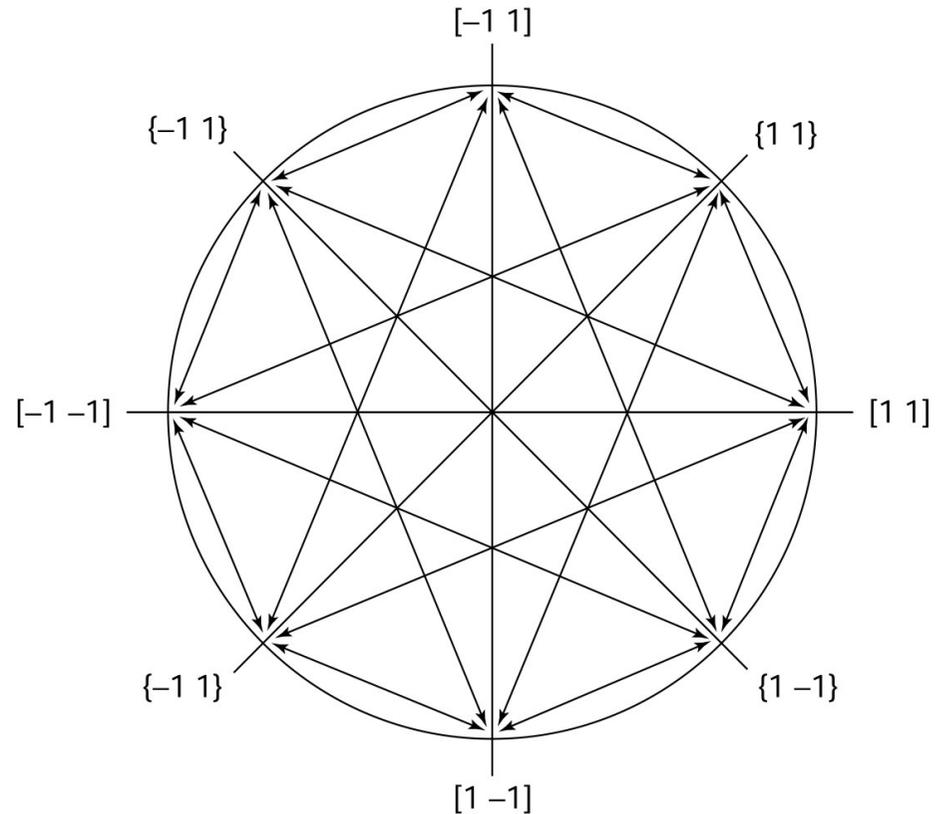
Eight possible phase states for the  $\pi/4$ -shifted QPSK modulator.



Phase encoding for  $\pi/4$ -QPSK. The brackets [ ] and { } correspond to the two respective constellations.

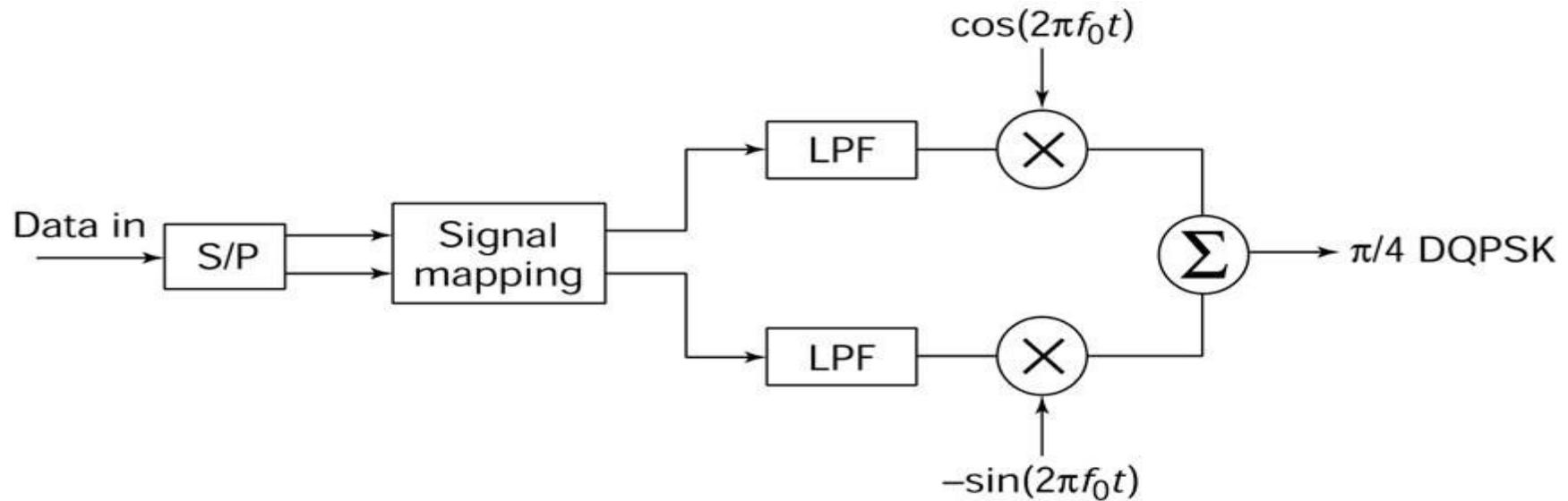


Details of the phase constellation associated with  $\pi/4$ -QPSK. For every alternate symbol, the carrier waves are changed. From (1,1) to (-1, -1), we go from [1 1] to {-1, -1}, or from {1,1} to [-1, -1], resulting in a phase change of  $3\pi/4$ , as opposed to  $\pi/2$  in QPSK. In QPSK we can go from [1, 1] to [-1, -1] or from {1 1} to {-1, -1}, resulting in a phase change of  $\pi$ . Also, when we go from (1, 1) to (1, 1) in  $\pi/4$ -QPSK, we go from [1, 1] to {1, 1}, resulting in a phase change of  $\pi/4$ . The phase changes in  $\pi/4$ -QPSK are limited to  $3\pi/4$  or  $\pi/4$ . There are no phase changes of  $0$ ,  $\pi/2$ , or  $\pi$ . All the possible transitions are shown by arrows.



$\pi/4$	$5\pi/4$	$3\pi/4$	$\pi/4$
1 1	-1 -1	-1 1	1 1
I Q	I Q	I Q	I Q

Block diagram of the  $\pi/4$ -DQPSK transmitter.



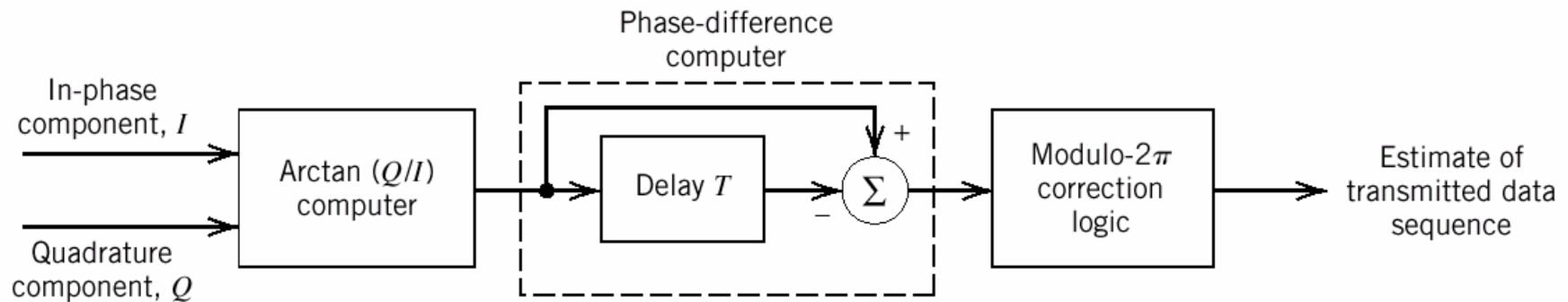
(b)

Input dibit	Phase change
00	$\pi/4$
01	$3\pi/4$
11	$-3\pi/4$
10	$-\pi/4$

$$\vartheta_k = \vartheta_{k-1} + \Delta$$

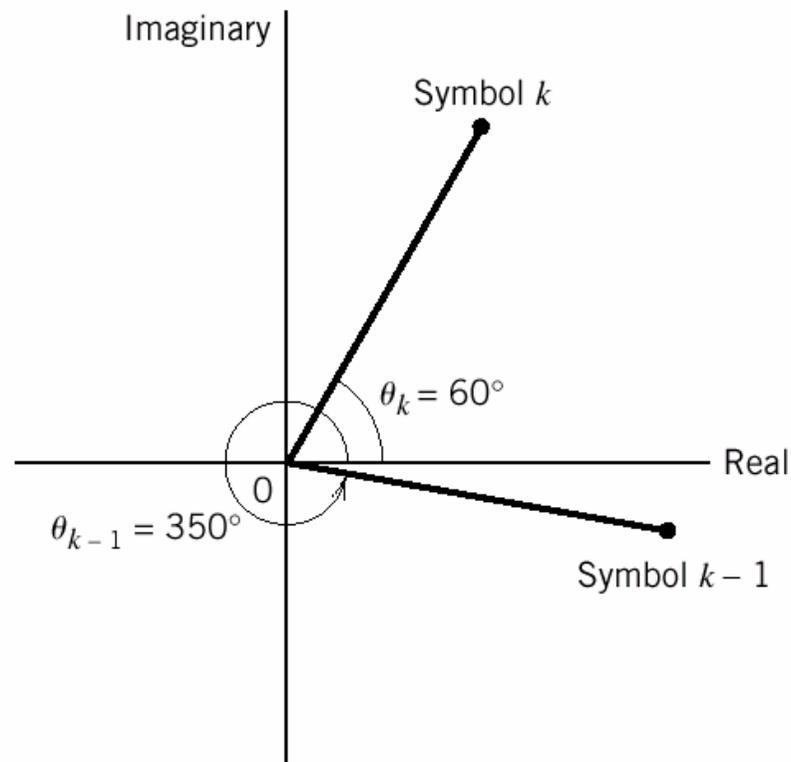
# Figure 6.13

Block diagram of the  $\pi/4$ -shifted DQPSK detector.



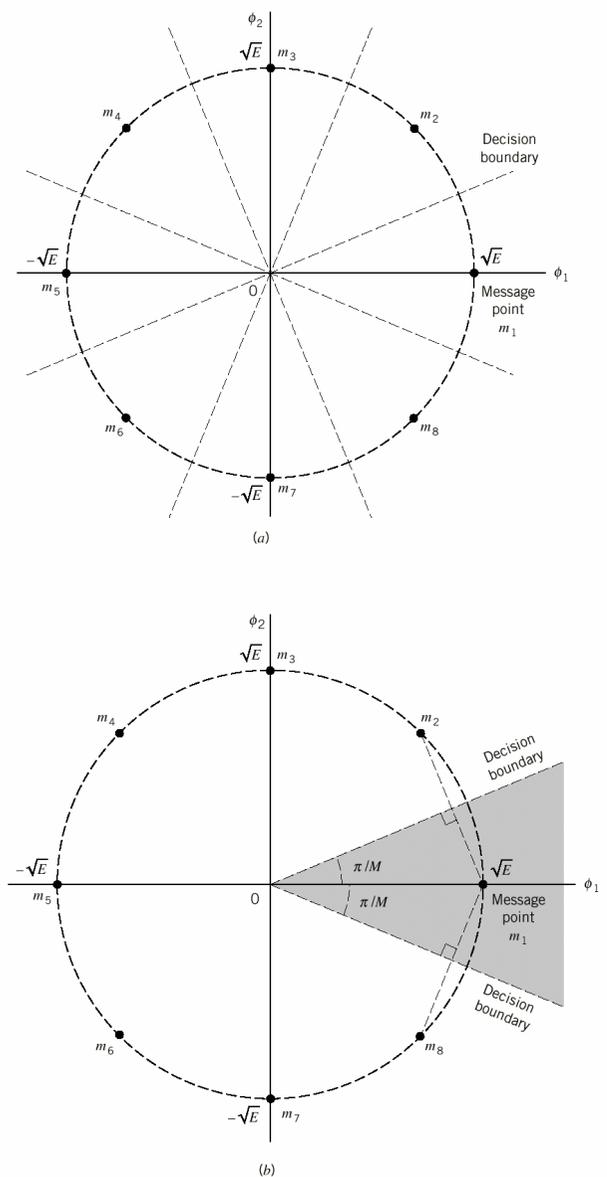
# Figure 6.14

Illustrating the possibility of phase angles wrapping around the positive real axis.



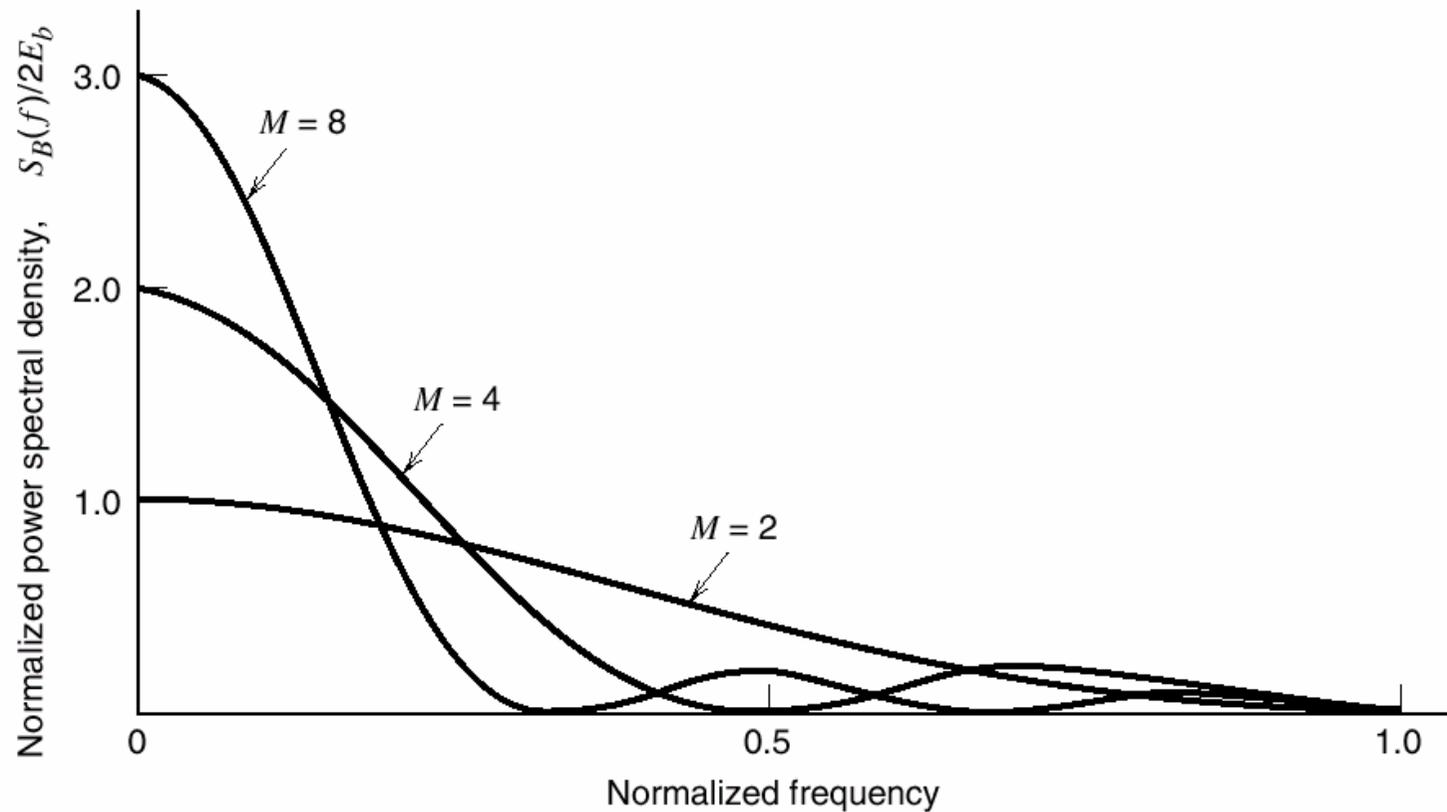
# Figure 6.15

(a) Signal-space diagram for octaphase-shift keying (i.e.,  $M = 8$ ). The decision boundaries are shown as dashed lines. (b) Signal-space diagram illustrating the application of the union bound for octaphase-shift keying.



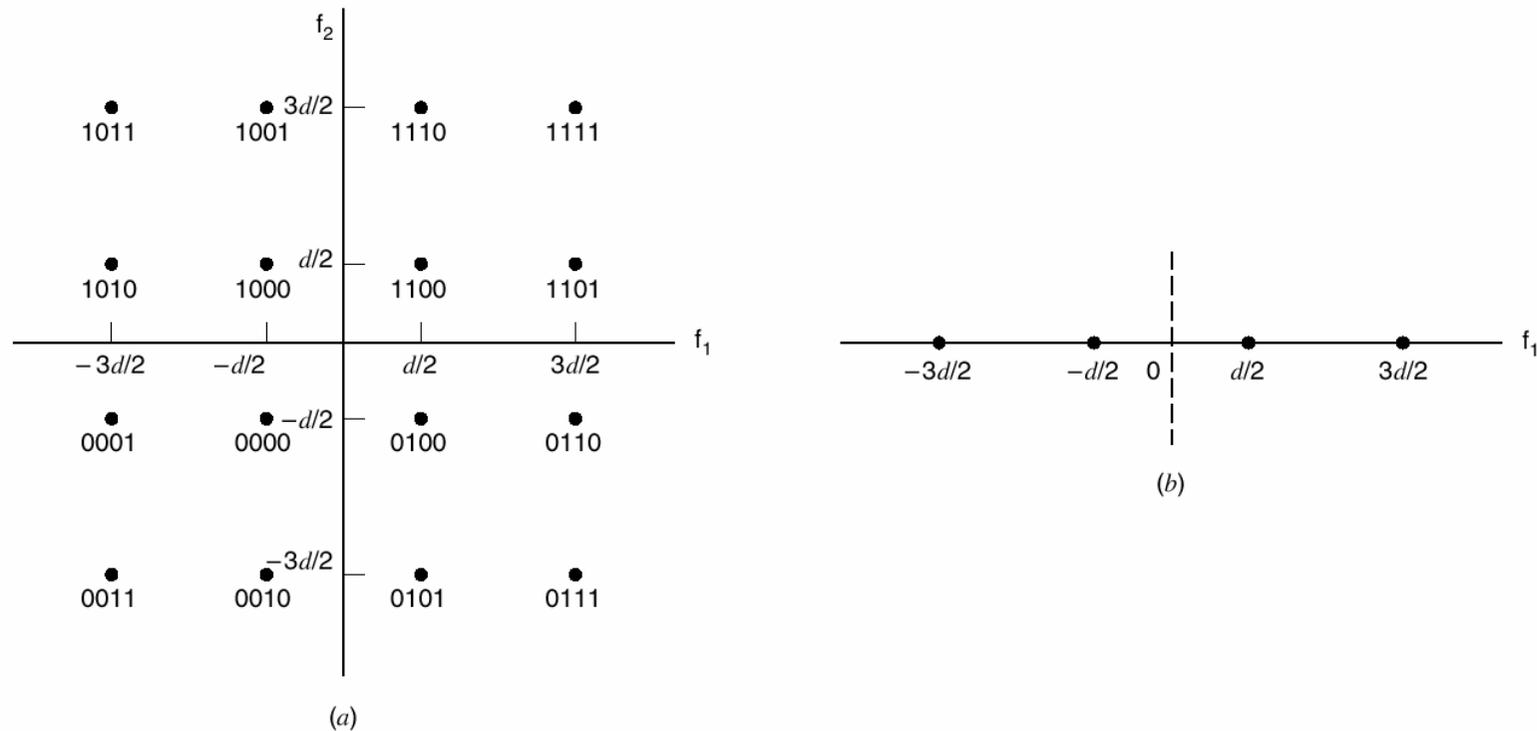
# Figure 6.16

Power spectra of  $M$ -ary PSK signals for  $M = 2, 4, 8$ .



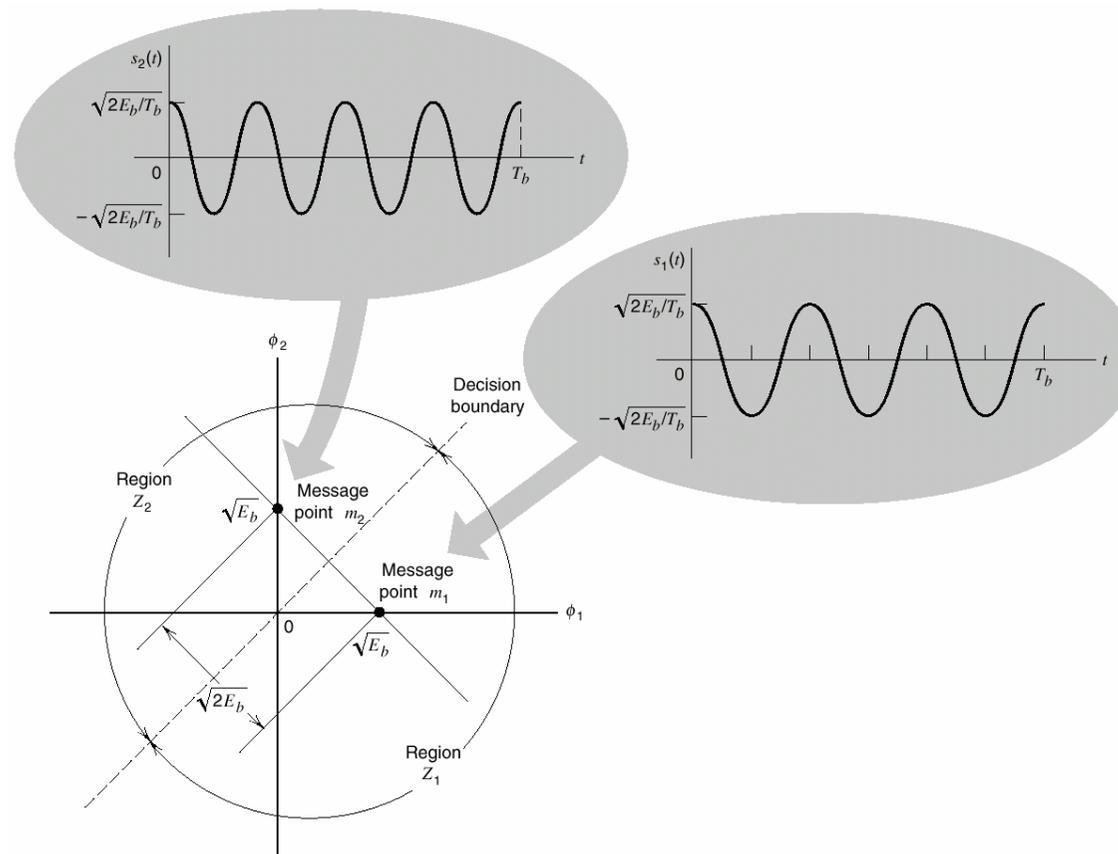
## Figure 6.17

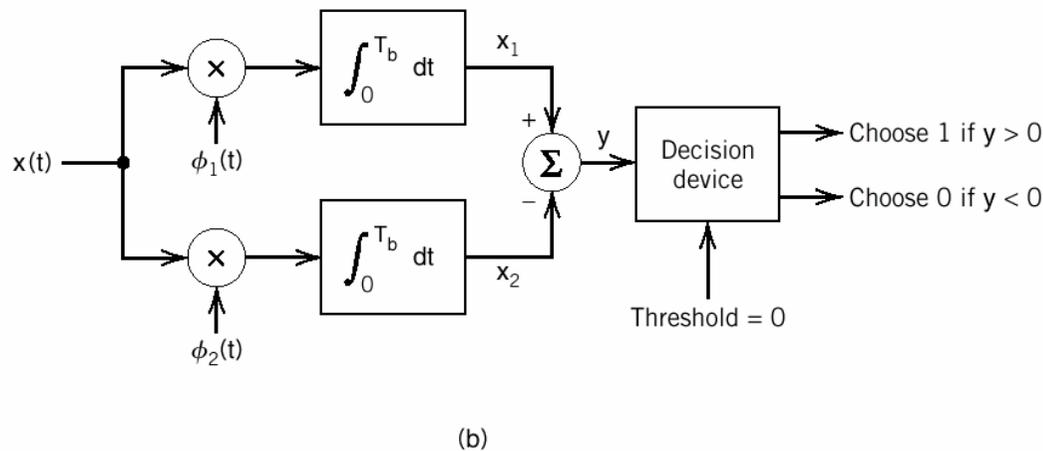
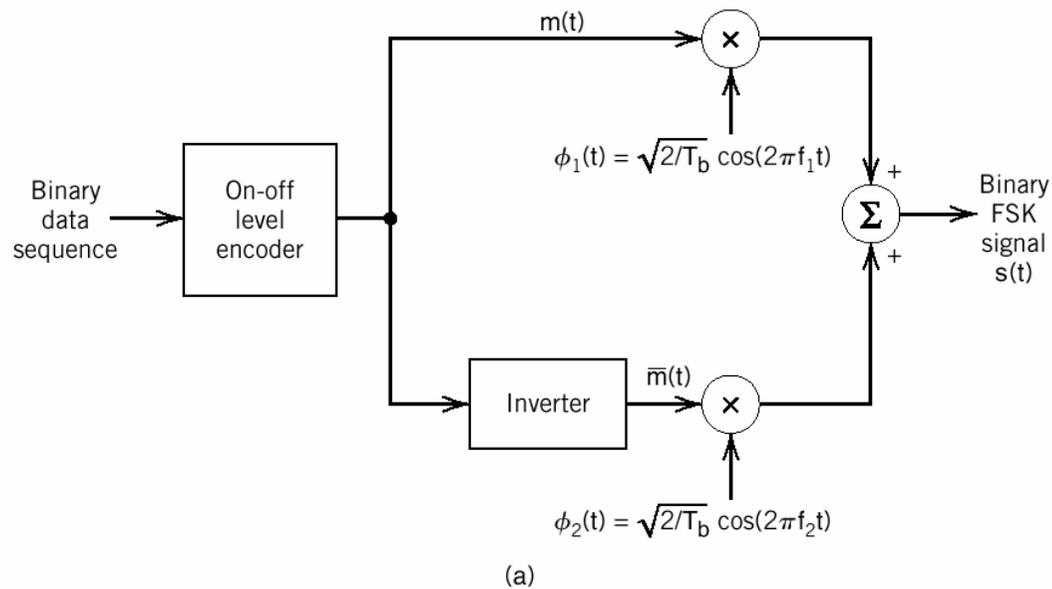
(a) Signal-space diagram of  $M$ -ary QAM for  $M = 16$ ; the message points in each quadrant are identified with Gray-encoded quadbits. (b) Signal-space diagram of the corresponding 4-PAM signal.



## Figure 6.25

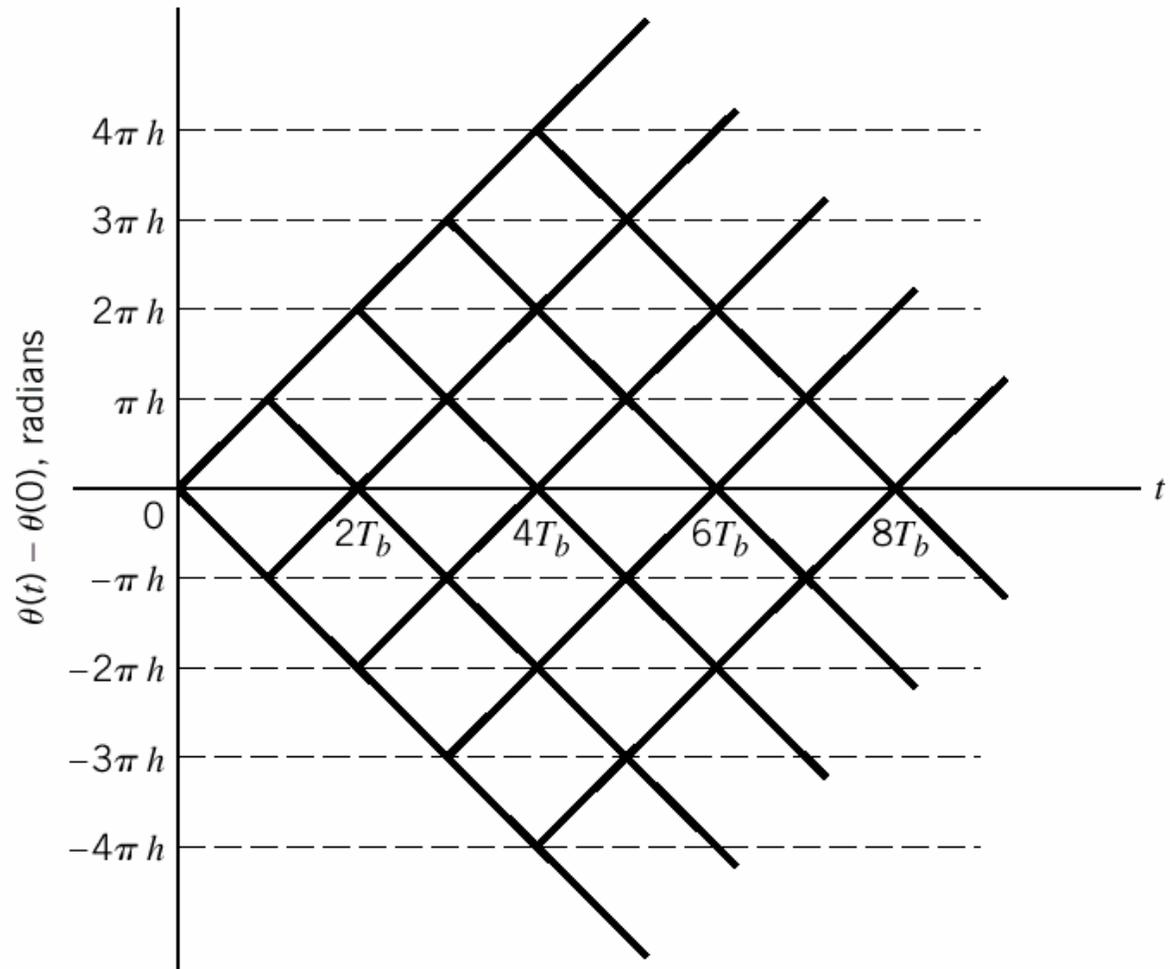
Signal-space diagram for binary FSK system. The diagram also includes two inserts showing example waveforms of the two modulated signals  $s_1(t)$  and  $s_2(t)$ .





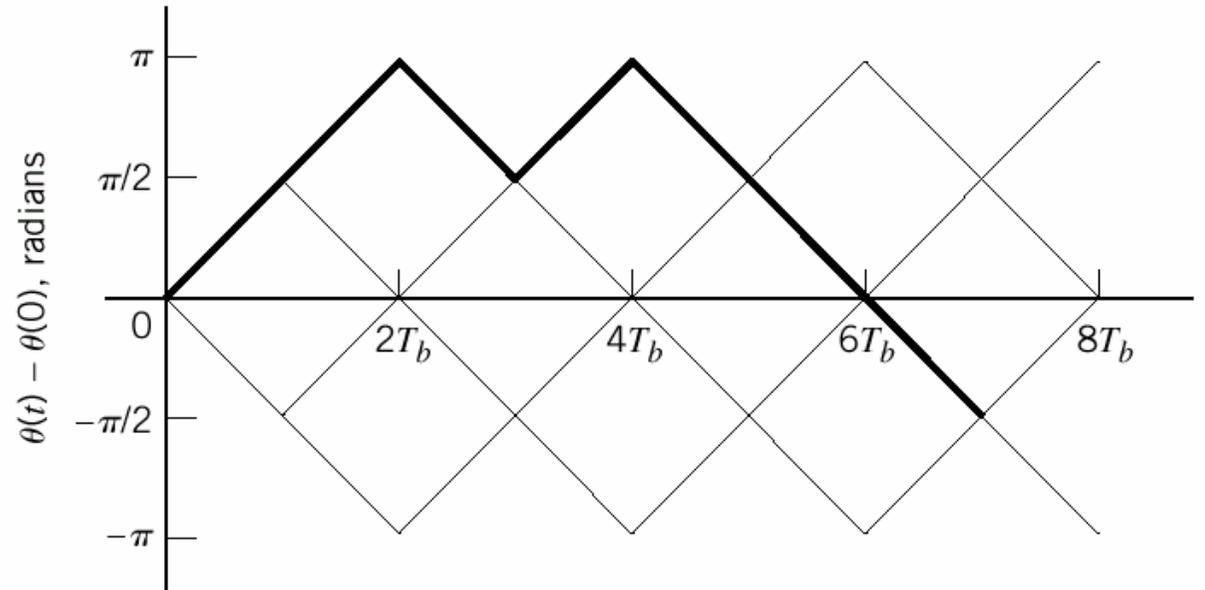
**Figure 6.26**  
Block diagrams for (a) binary FSK transmitter and (b) coherent binary FSK receiver.

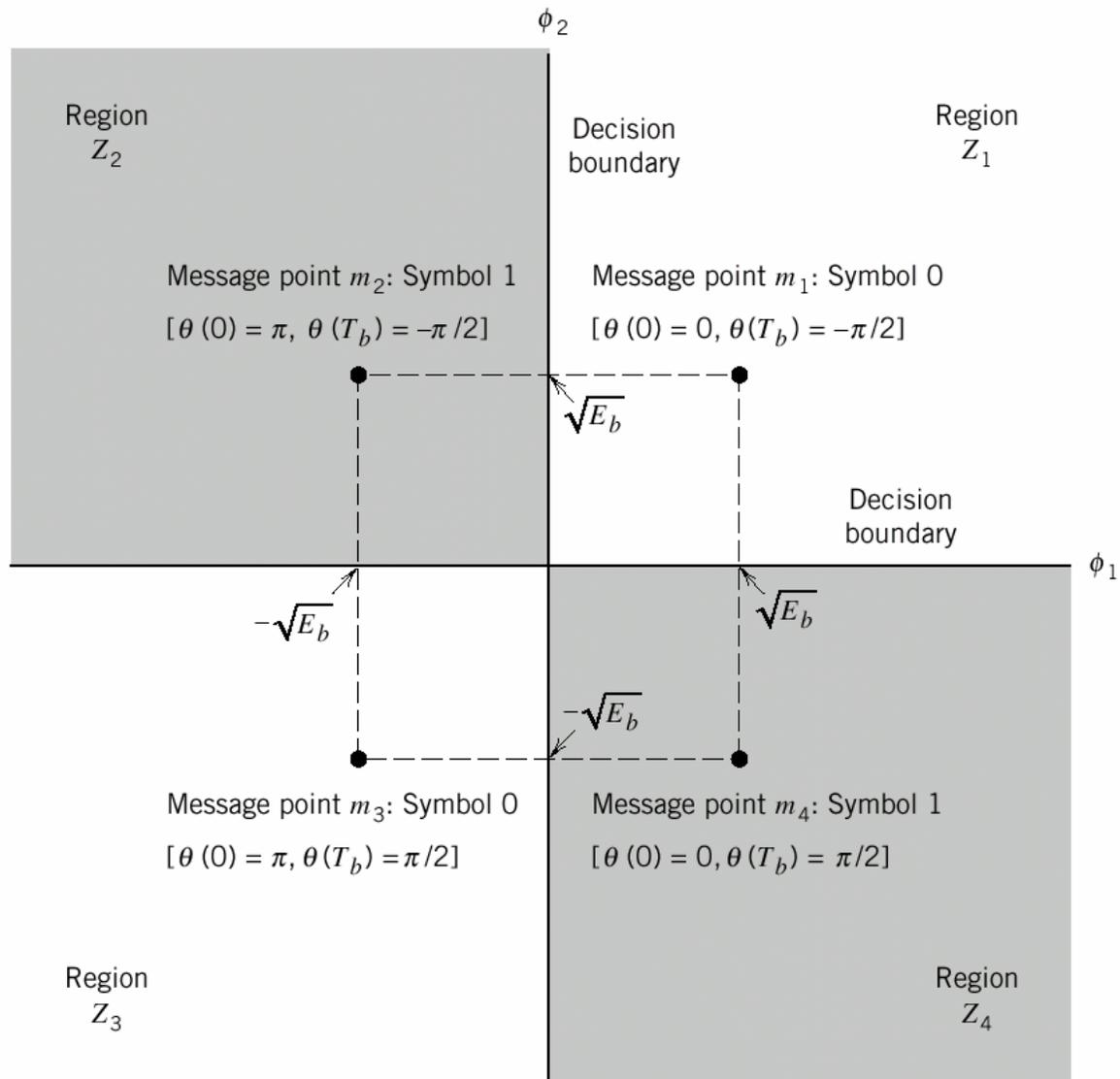
**Figure 6.27**  
Phase tree of  
CFM.



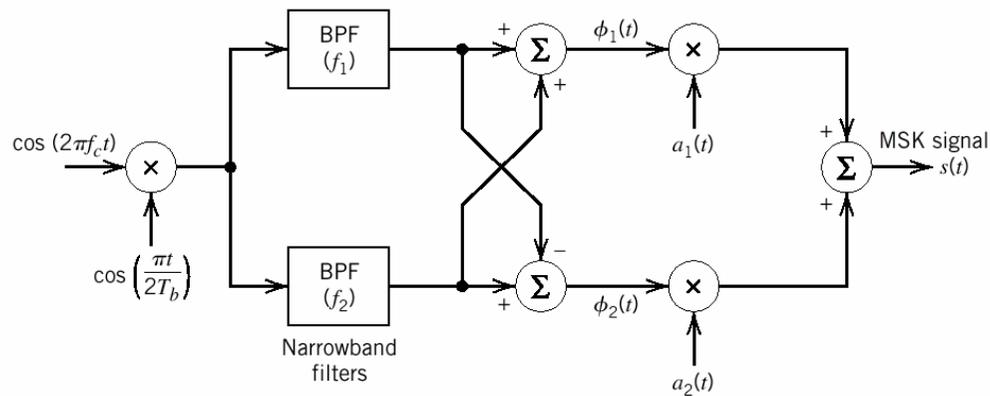
# Figure 6.28

Phase trellis; boldfaced path represents the sequence 1101000.

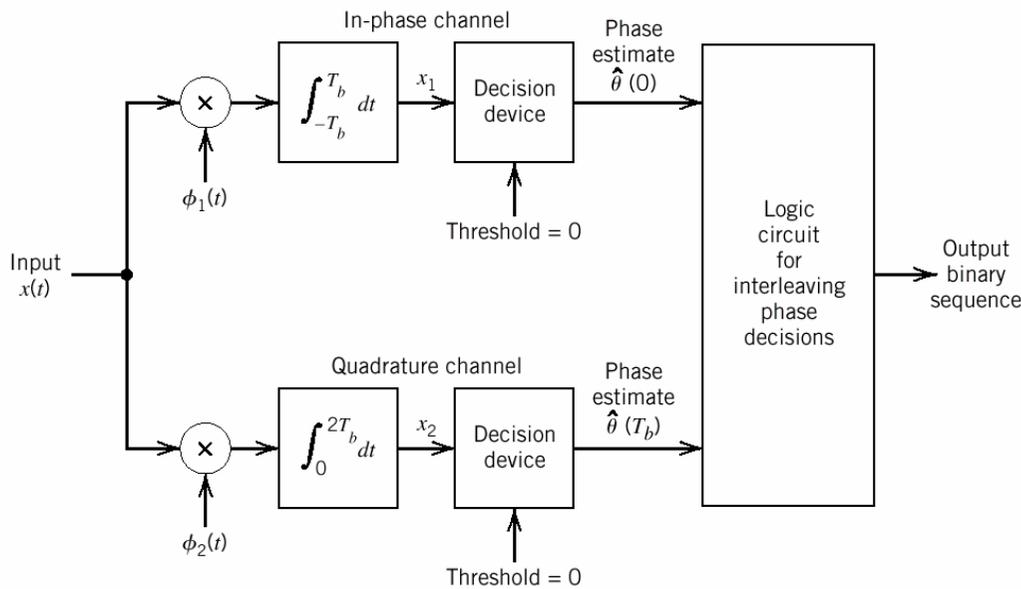




**Figure 6.29**  
Signal-space diagram for MSK system.



(a)

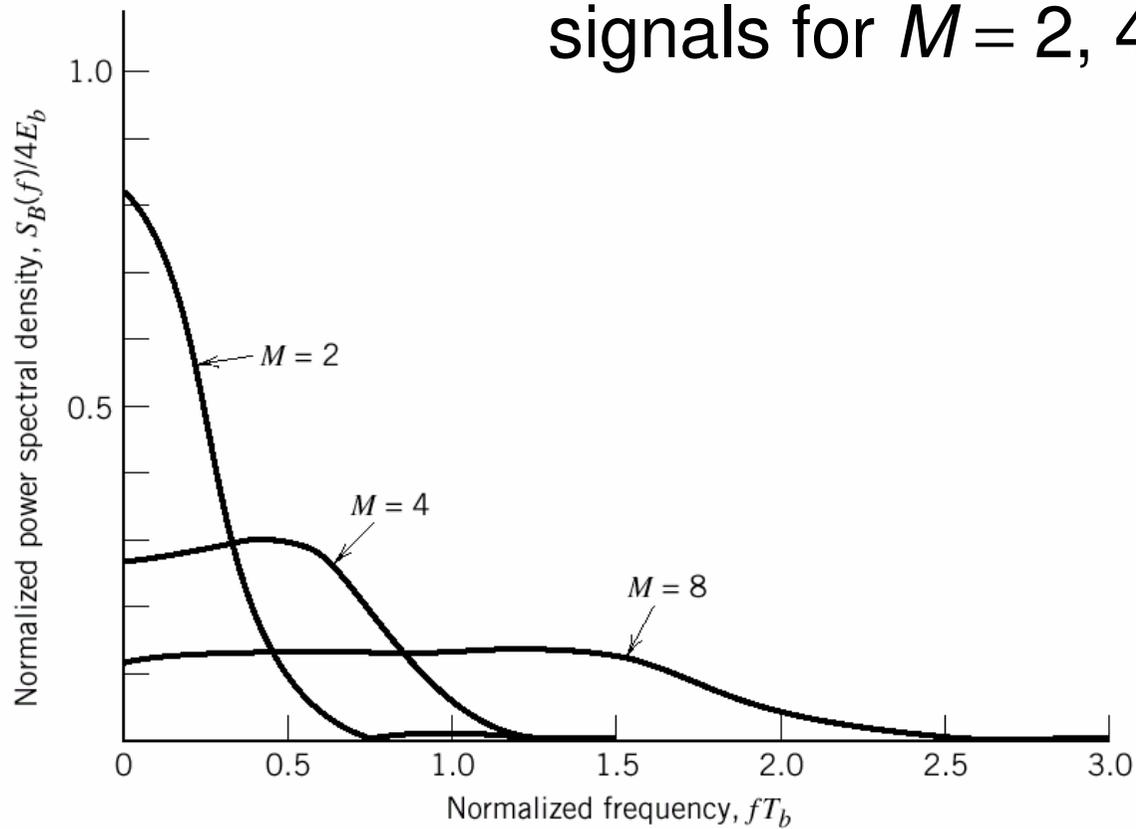


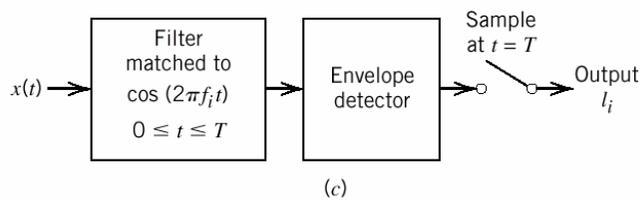
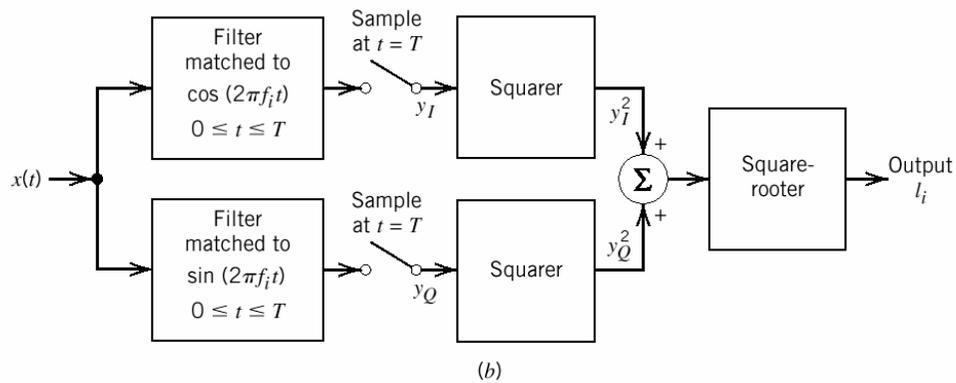
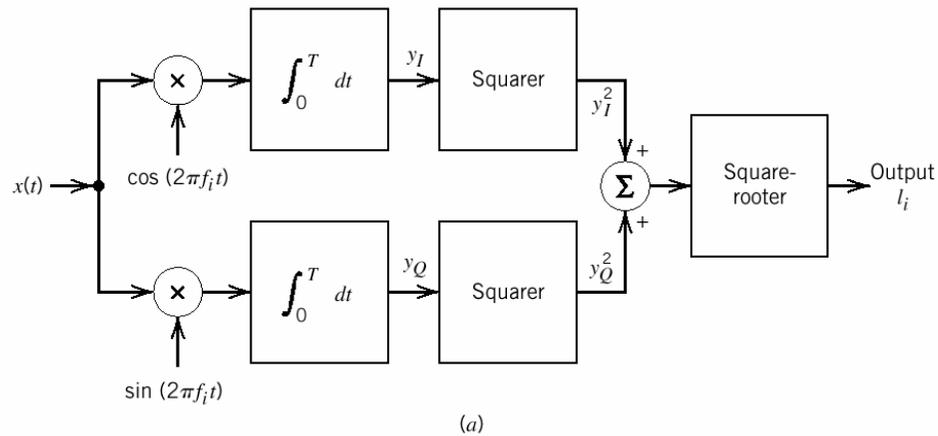
(b)

**Figure 6.31**  
Block diagrams  
for (a) MSK  
transmitter and  
(b) coherent  
MSK receiver.

## Figure 6.36

Power spectra of  $M$ -ary FSK signals for  $M = 2, 4, 8$ .





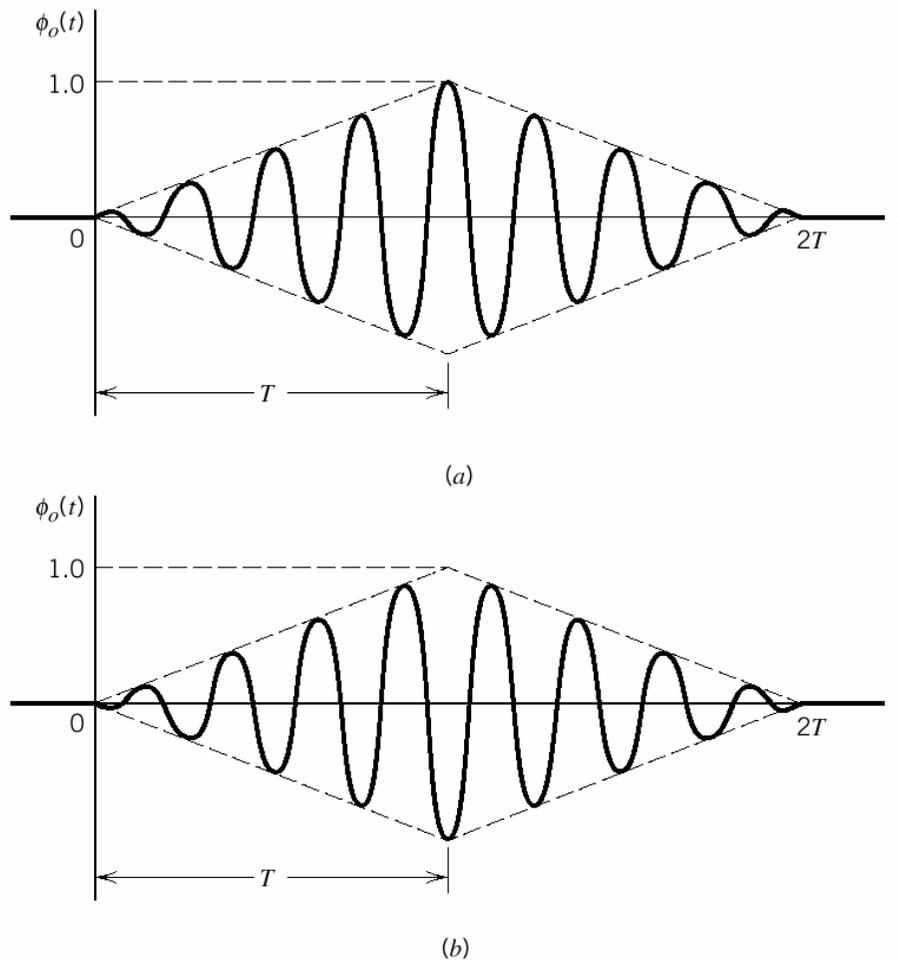
**Figure 6.37**

Noncoherent receivers.

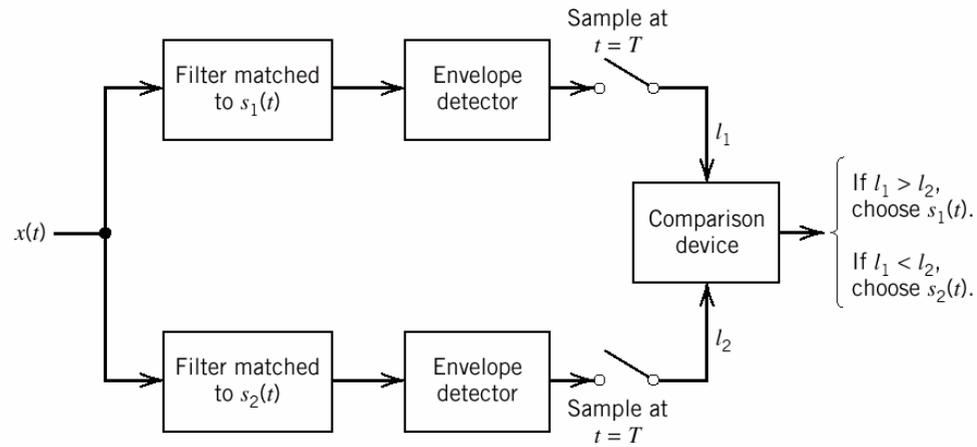
(a) Quadrature receiver using correlators.

(b) Quadrature receiver using matched filters.

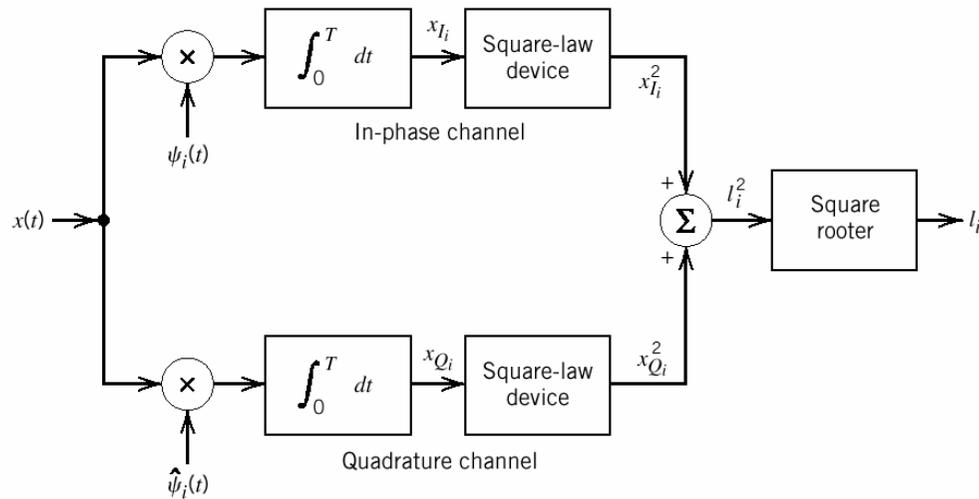
(c) Noncoherent matched filter.



**Figure 6.38**  
 Output of matched filter for a rectangular RF wave: (a)  $\theta = 0$ , and (b)  $\theta = 180$  degrees.



(a)



(b)

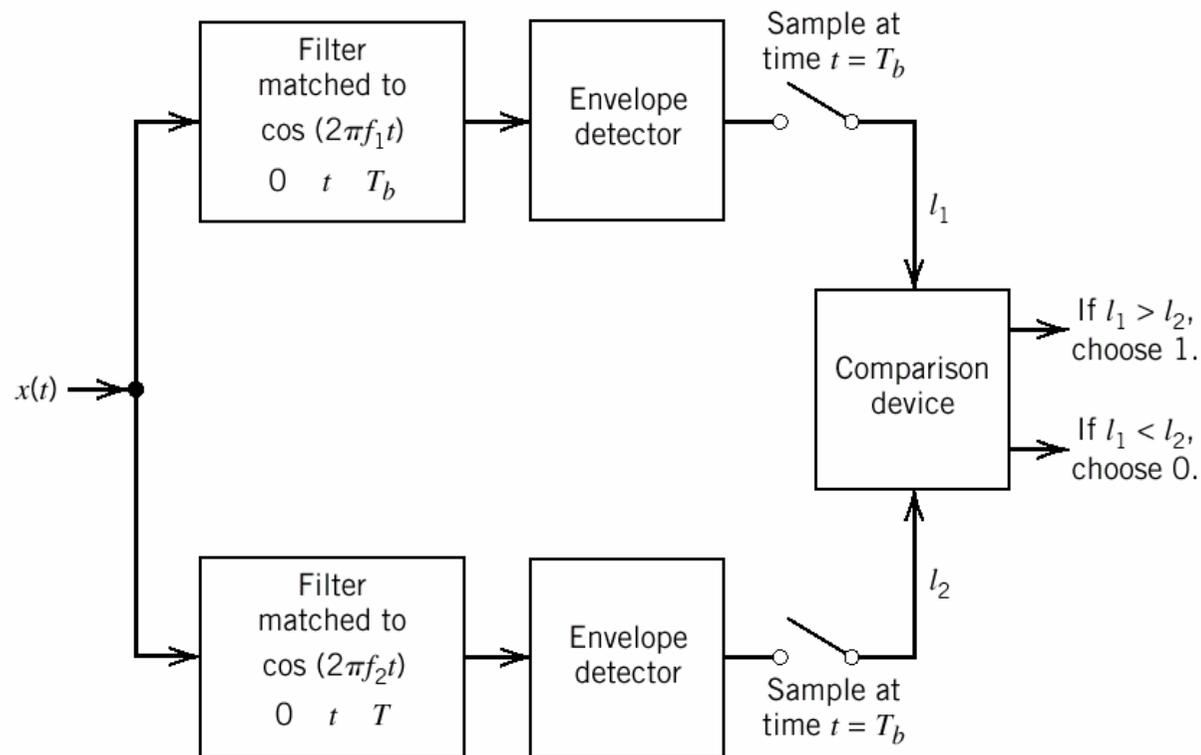
## Figure 6.39

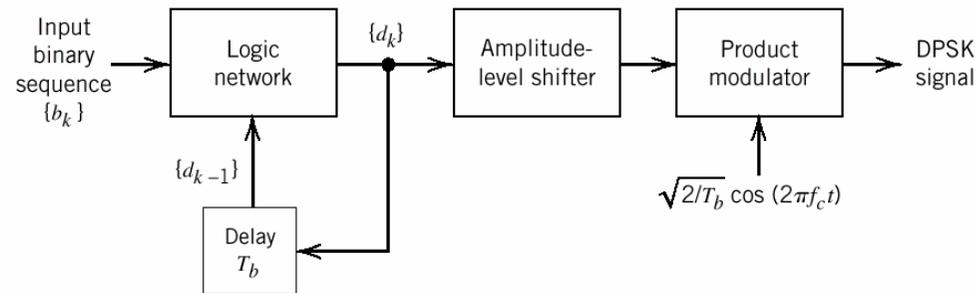
(a) Generalized binary receiver for noncoherent orthogonal modulation.

(b) Quadrature receiver equivalent to either one of the two matched filters in part (a); the index  $i = 1, 2$ .

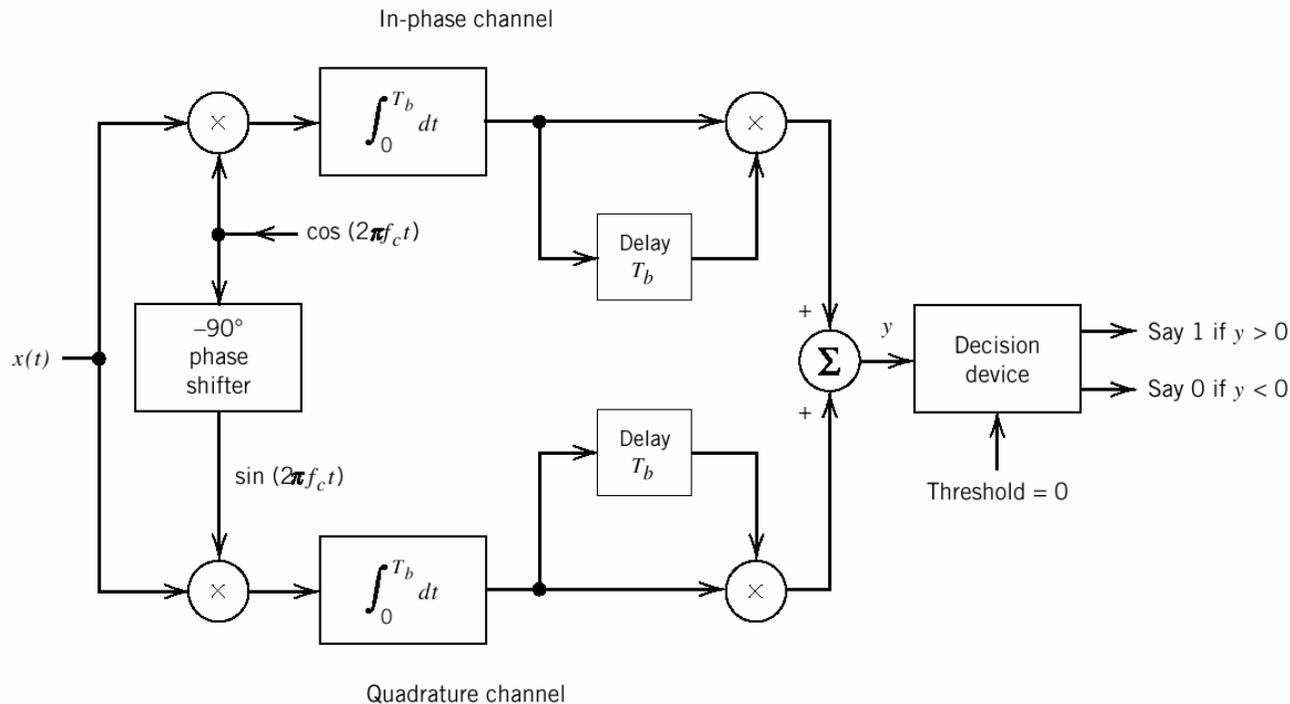
# Figure 6.42

Noncoherent receiver for the detection of binary FSK signals.





(a)

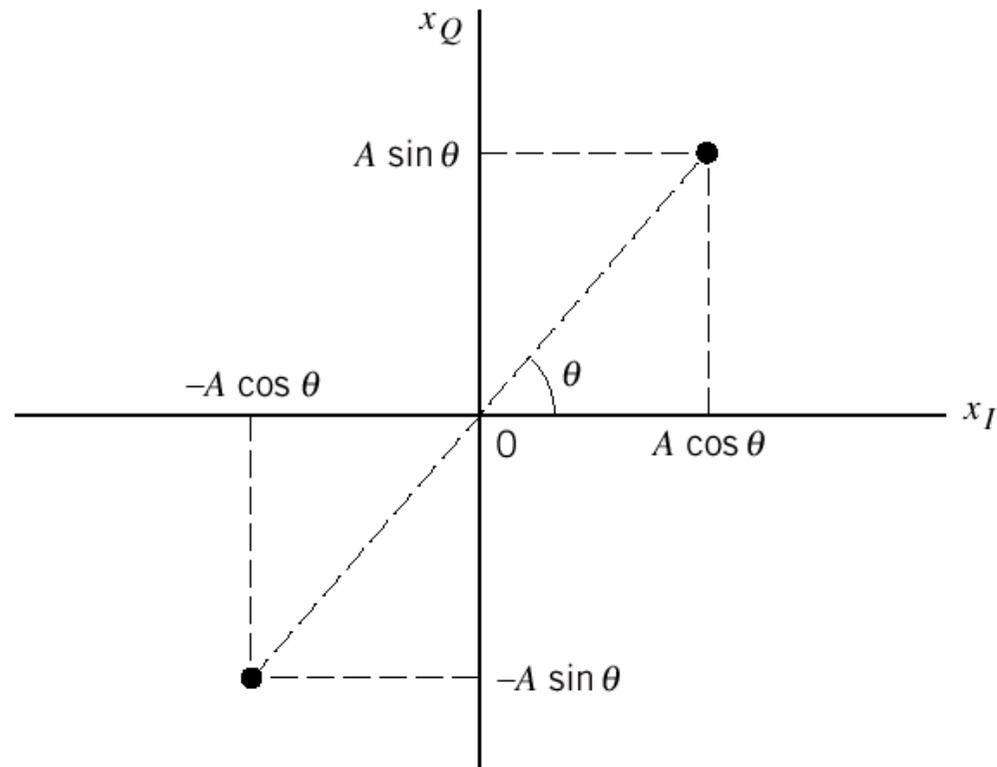


(b)

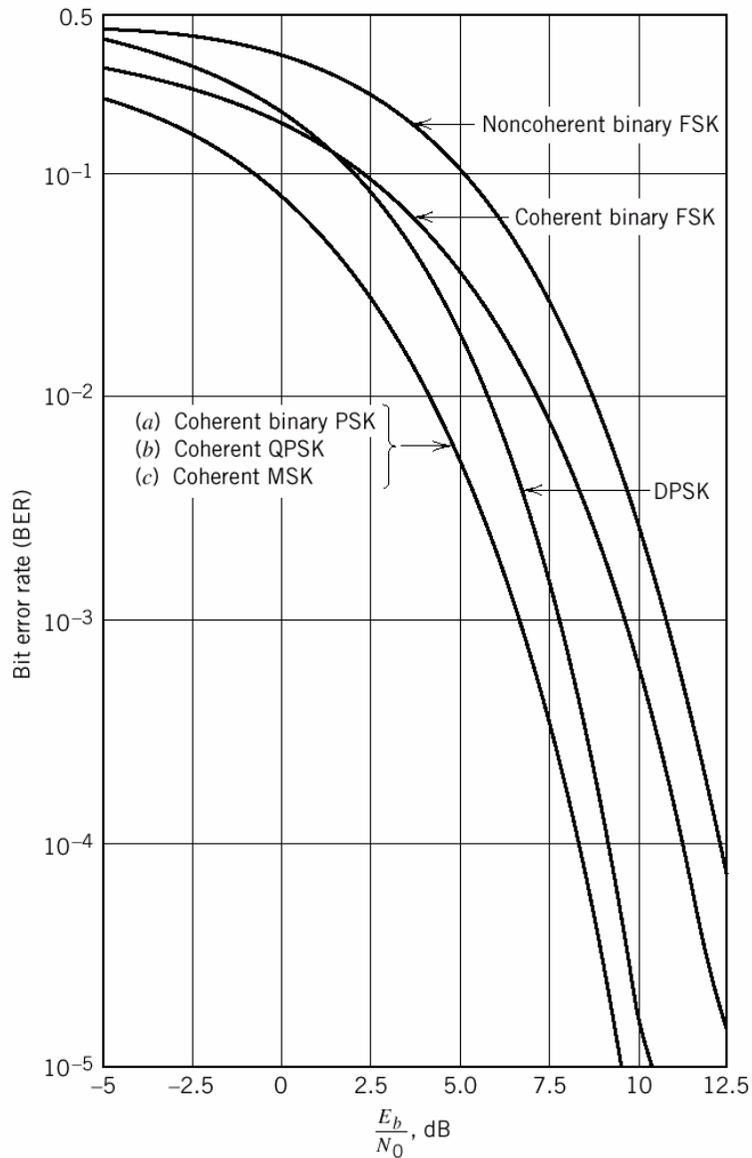
**Figure 6.43**  
Block diagrams of (a) DPSK transmitter and (b) DPSK receiver.

# Figure 6.44

Signal-space diagram of received DPSK signal.



- ML slides



**Figure 6.45**  
 Comparison of the noise performance of different PSK and FSK schemes.

